

EFFICIENT MULTI-PHYSICS MODELING OF THE DYNAMIC RESPONSE OF RF-MEMS SWITCHES

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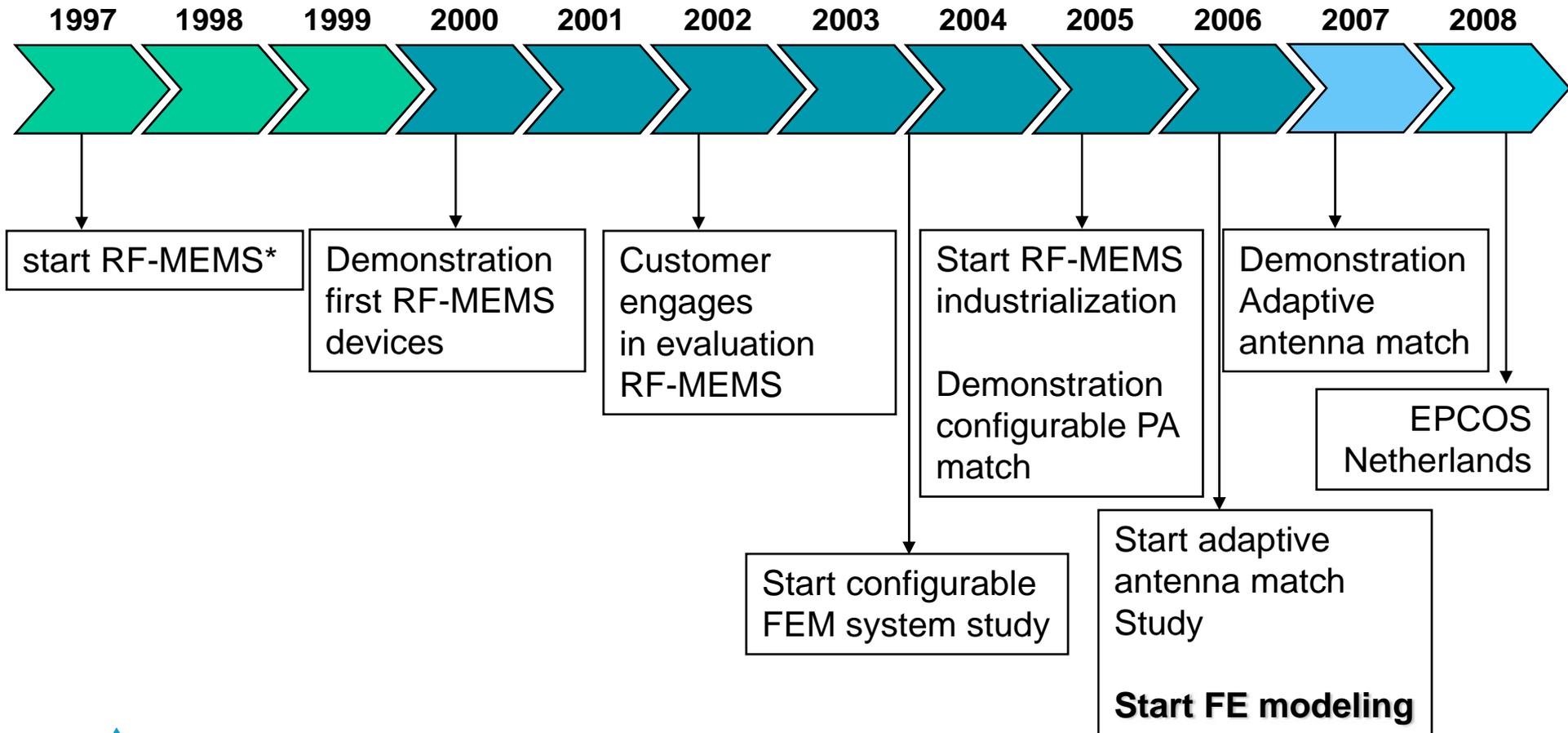
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- Intro RF-MEMS at EPCOS Netherlands
- Physics of capacitive MEMS switch
- FE model:
 - Coupling of physics domains
 - Obtaining the static solution
 - Homogenization of surface roughness
 - Non-linear Reynolds for fluid / large signal transient
- Transient results & calibration with measurement
- Conclusion & outlook

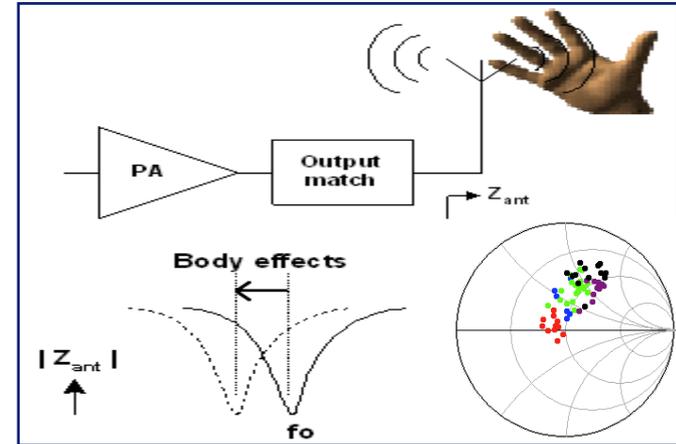
History of RF-MEMS and tuneable RF systems



* Program started at Philips Research

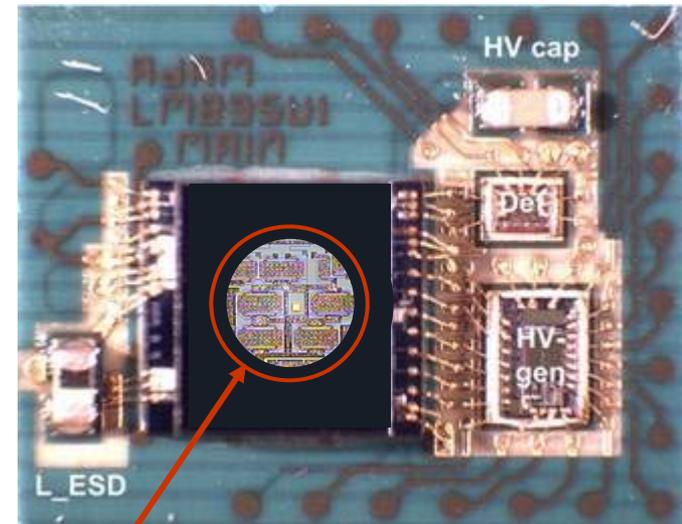
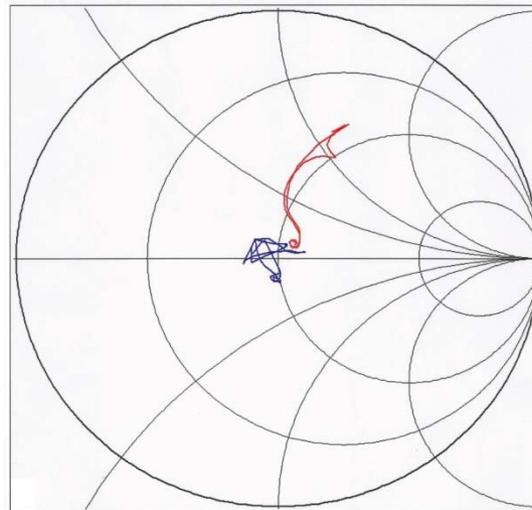
Adaptive multi-band antenna optimized performance

- A plug and play antenna module
 - frequency band configurable
 - automatic performance optimization
- increased average RF output power
- increased battery time
- lower VSWR, more system margin



Measurement data LB:

- uncorrected hand effects
- hand effects corrected by AdAM



Multiphysics modeling required



EPCOS Efficient multi-physics modeling of the dynamic response of RF-MEMS switches



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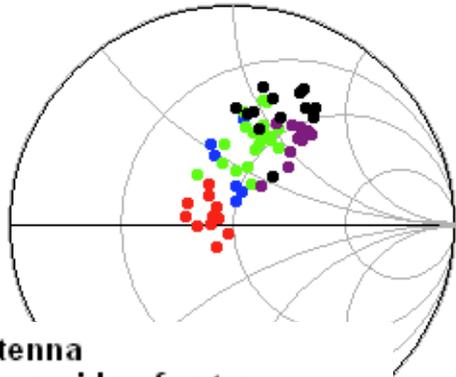


NAFEMS 2020 Vision of Engineering Analysis and Simulation

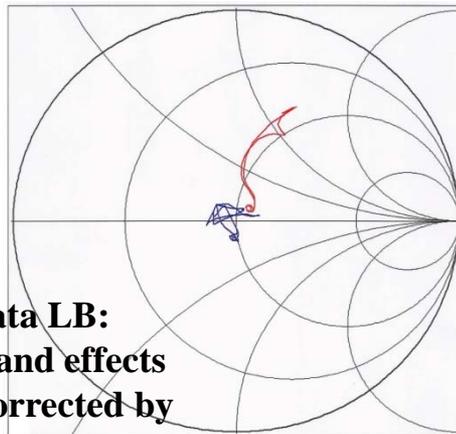


Introduction RF-MEMS: Application example

Hand detuning effects effectively corrected – AdAM

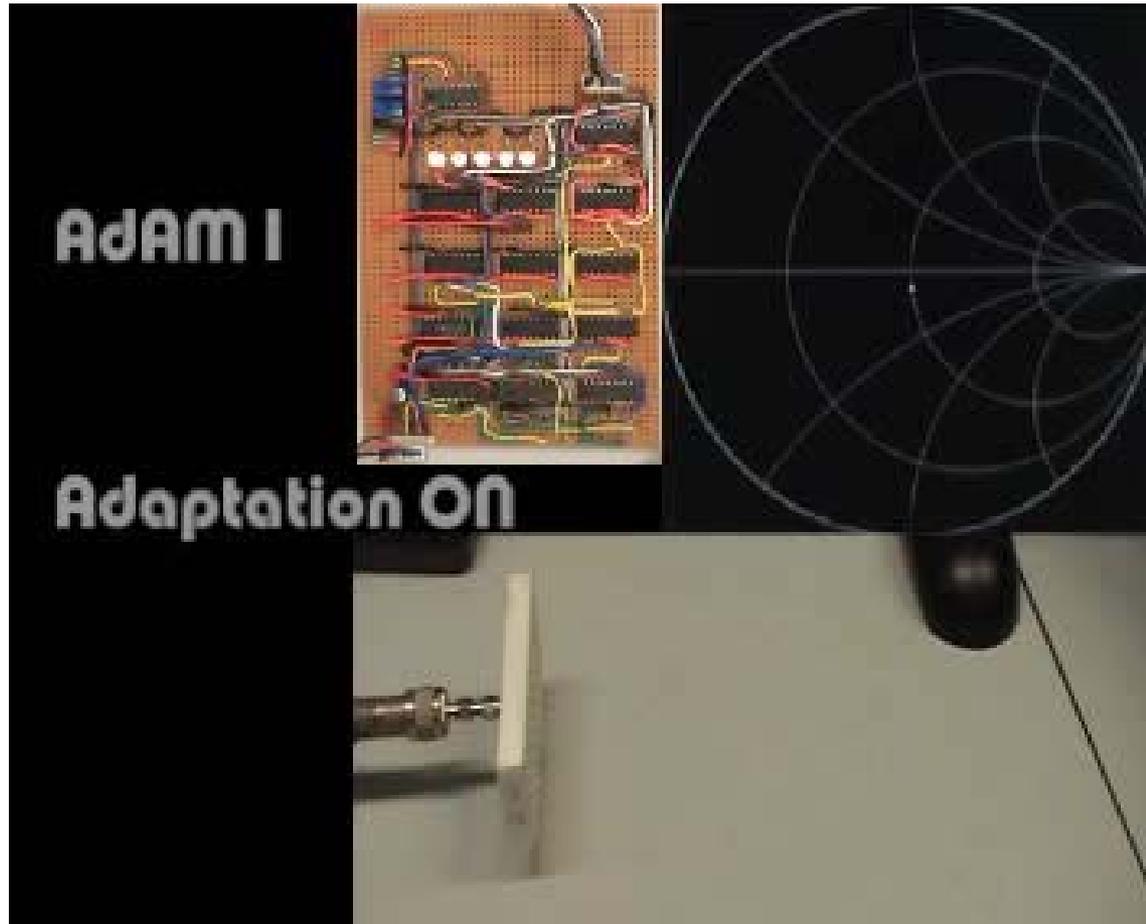


- hand not on antenna
- thumb or finger on side of antenna
- thumb and fingers on side of antenna
- hand and/or fingers on antenna
- hand and/or fingers over top of antenna



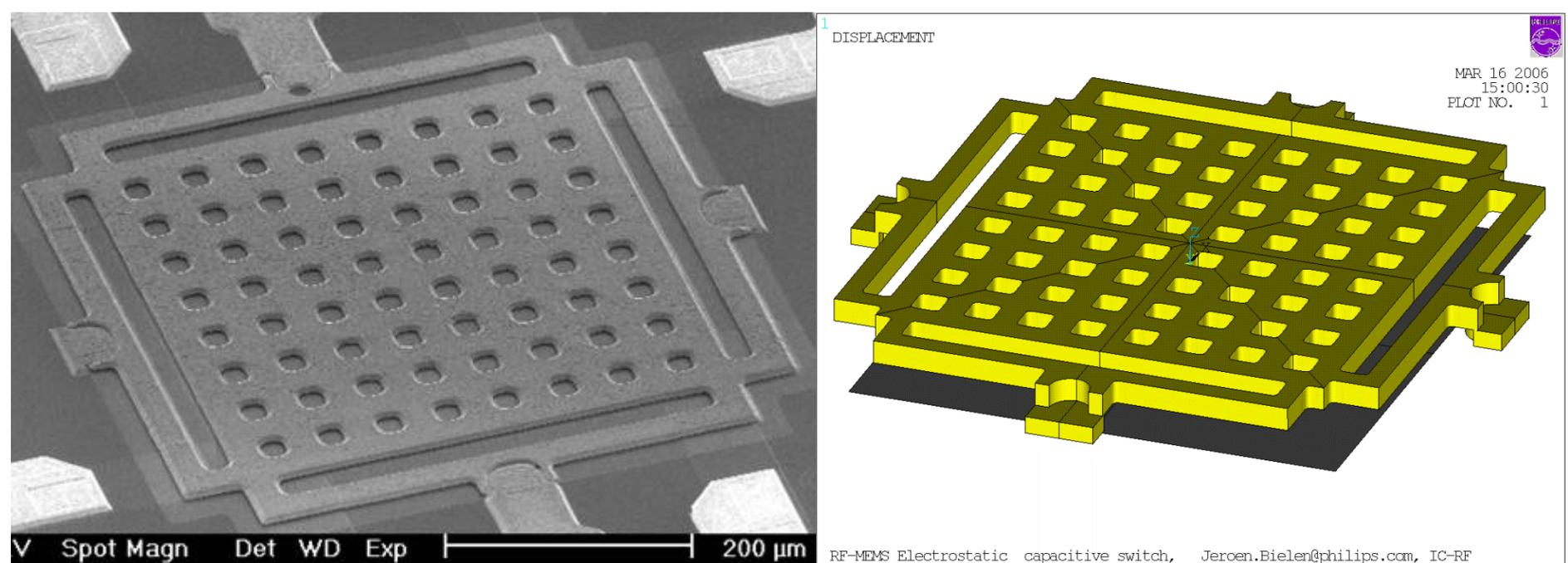
Measurement data LB:

- uncorrected hand effects
- hand effects corrected by AdAM-1 module



RF-MEMS capacitive switch

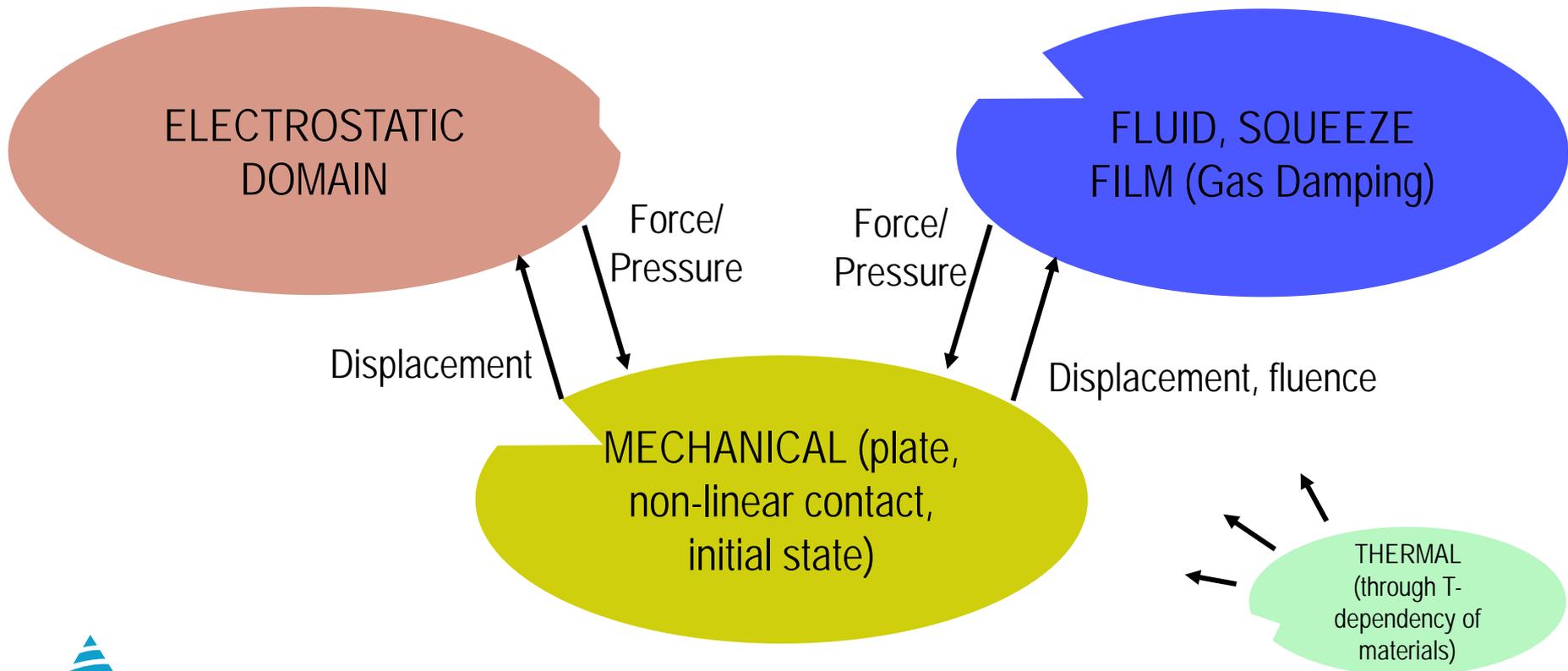
- Plate suspended by beams above bottom electrode covered with dielectric
- When a DC voltage is supplied the plate is pulled-down thus creating a 20x larger capacitance between the electrodes



Finite element model: key to predictive design

Capacitive switch is multi-physics problem:

- Bi-directional coupling between three different physics domains
- Non-linearities cause pull-in instability and convergence problems

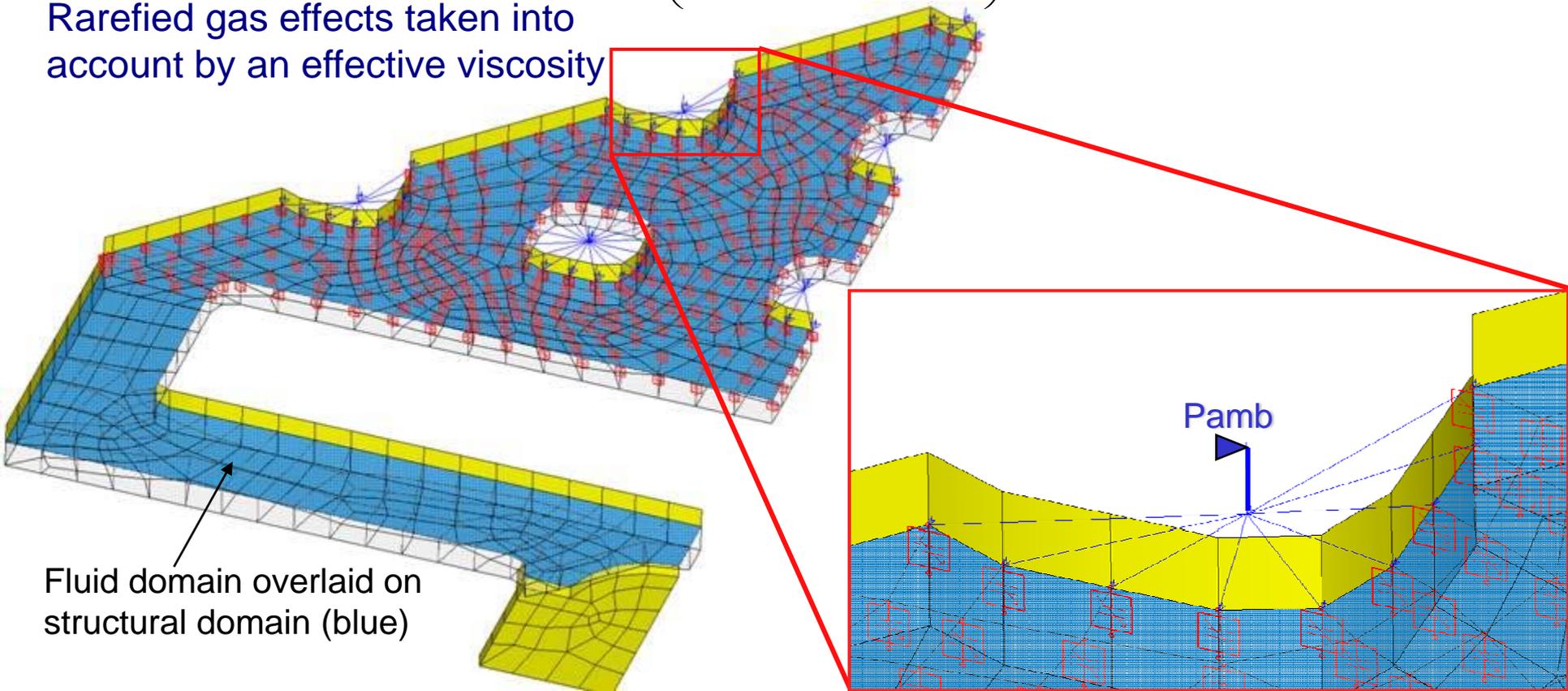


Directly coupled fluid-electro-mechanical model

Fluid-mechanical coupling with iso-thermal non-linear compressible Reynolds equation in directly coupled element:

$$\frac{H}{p} \frac{\partial p}{\partial t} + \frac{\partial H}{\partial t} = \frac{H^3}{p12\mu} \left(\left(\frac{\partial p}{\partial x} \right)^2 + \left(\frac{\partial p}{\partial y} \right)^2 \right) + \frac{H^3}{12\mu} \nabla^2 p$$

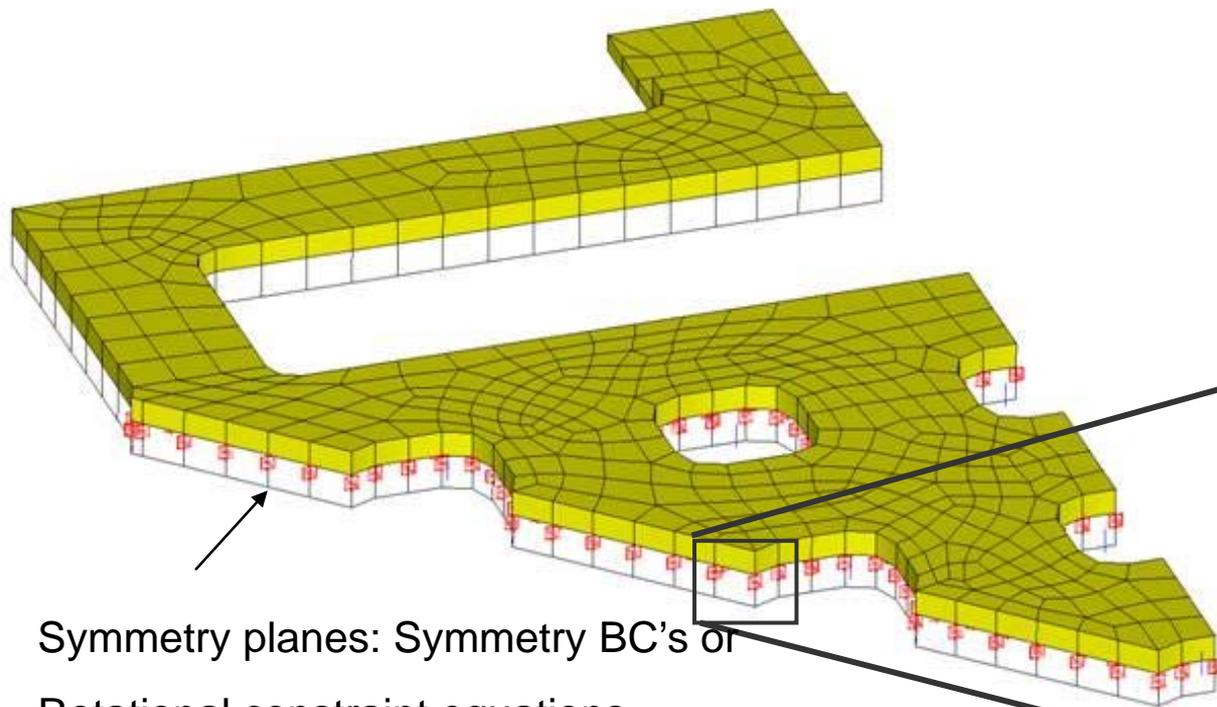
Rarefied gas effects taken into account by an effective viscosity



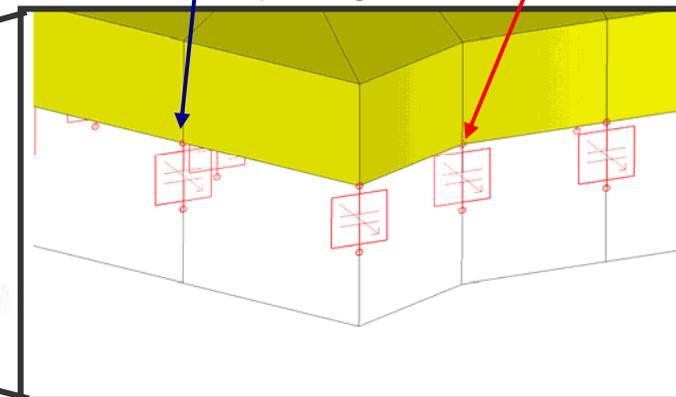
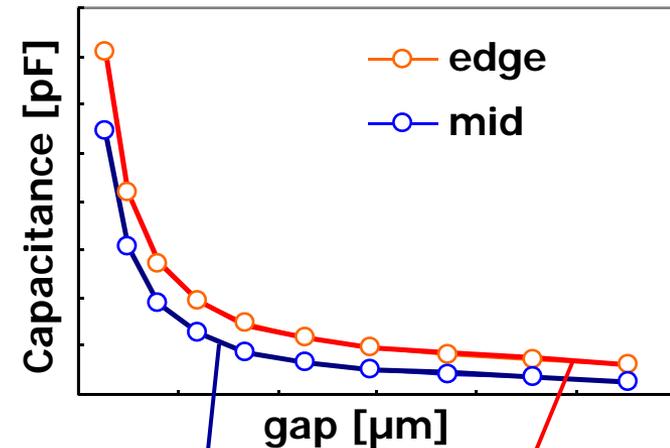
Fluid domain overlaid on structural domain (blue)

Directly coupled electro-mechanical model

- Electro-mechanical coupling very efficient with transducer elements (only one mechanical DOF & 1 Volt DOF per node)
- $C(z)$ of transducers from prior electrostatic simulation

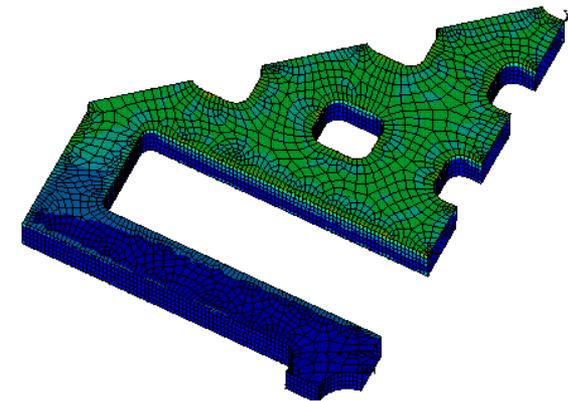
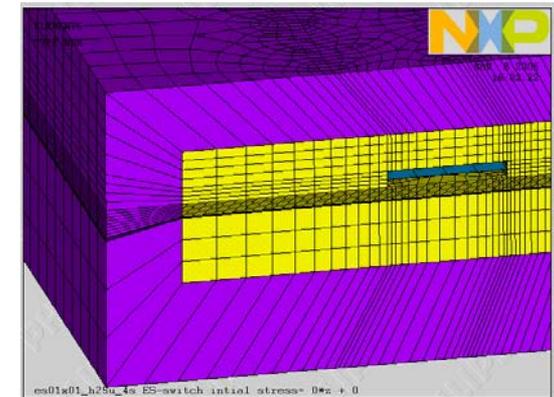
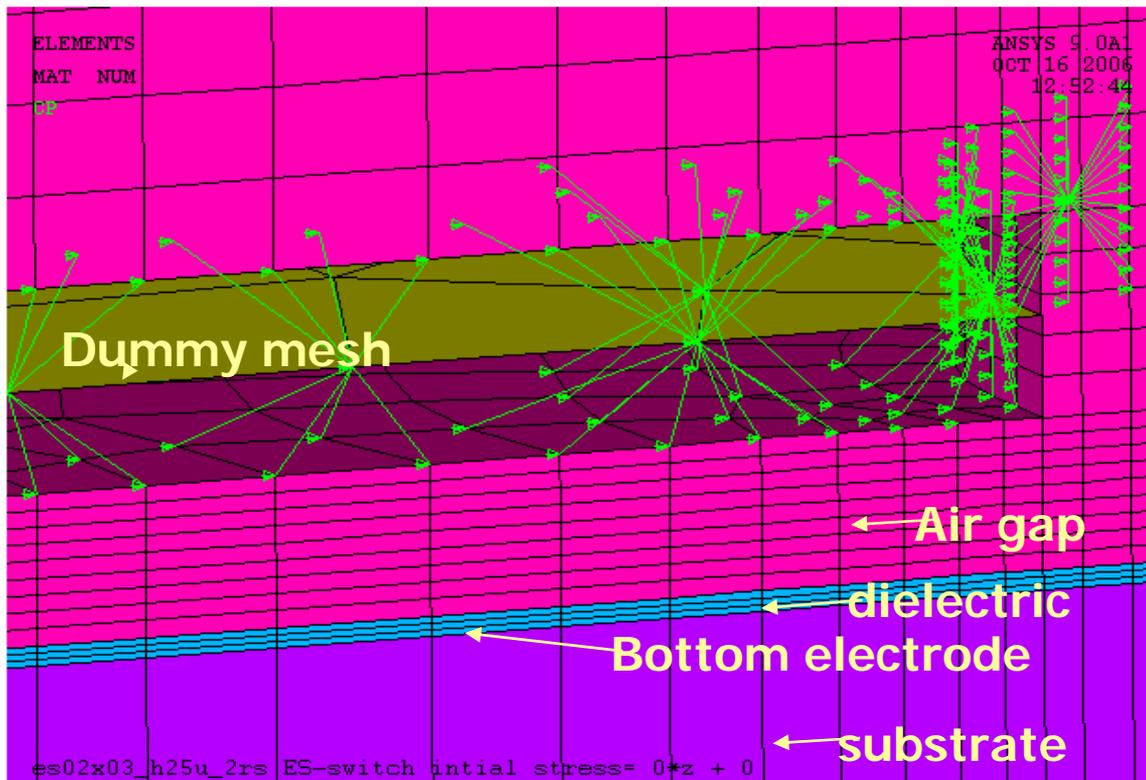


Symmetry planes: Symmetry BC's or
Rotational constraint equations



Electrostatic model

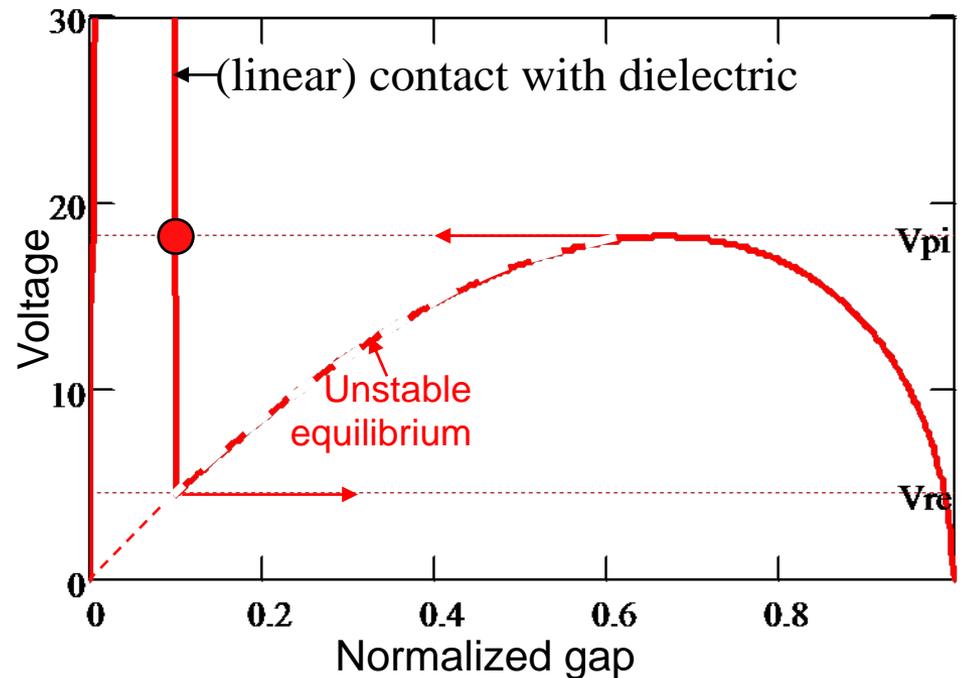
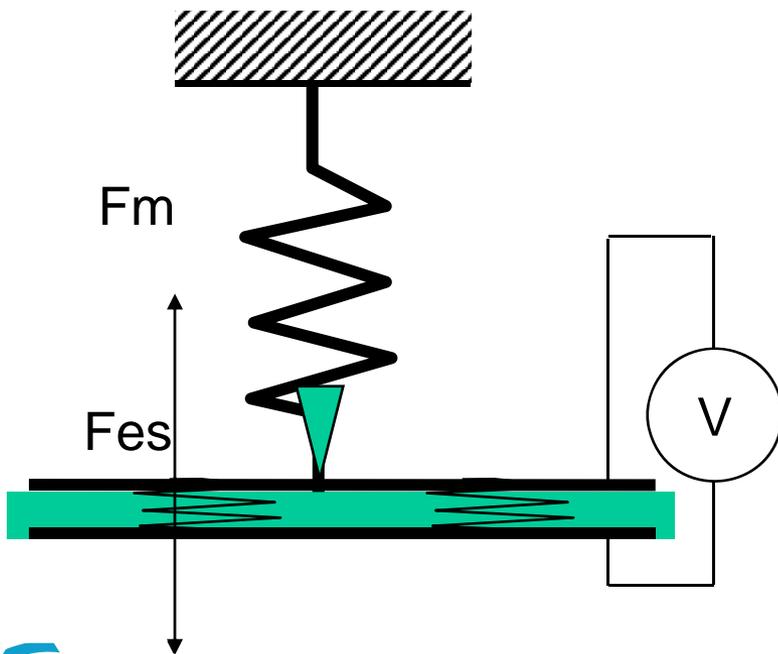
- Dummy mesh used to map charge from electrostatic mesh to nearest mechanical node allows for dissimilar meshes
- Electrostatic simulation repeated for various (uniform) gap heights



Solving Pull-in instability: DIPIE+

- Displacement iterations scheme (DIPIE) can solve pull-in instability because for every displacement there is only one voltage solution

$$F_m + F_{es} = k \cdot (z - \text{gap}_0) + \frac{\epsilon_0 \cdot \text{Area} \cdot V^2}{2 \cdot z^2} = 0$$

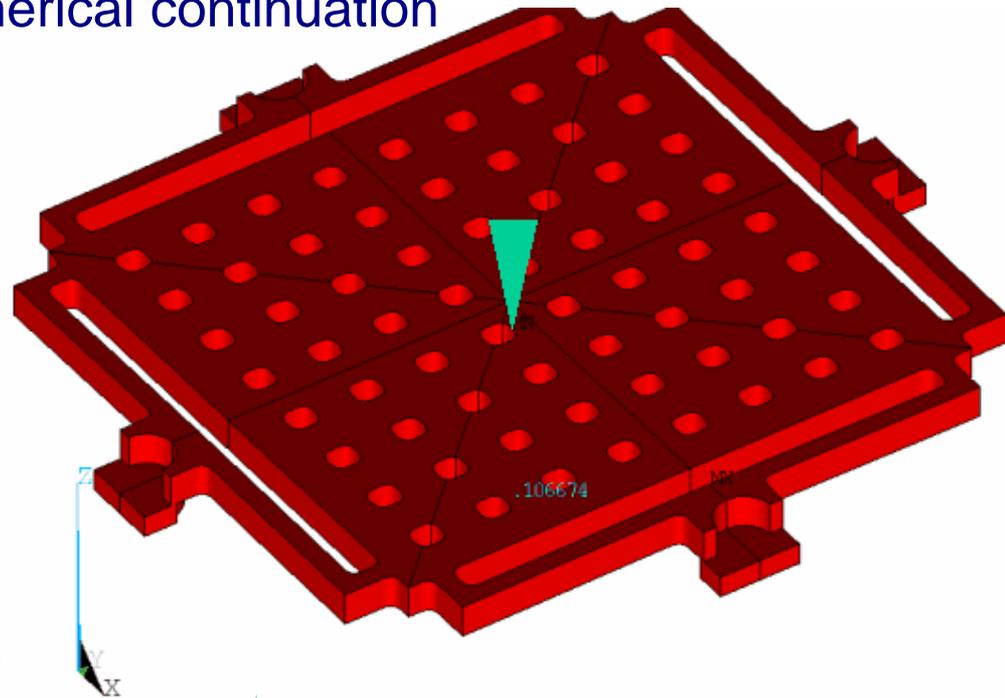
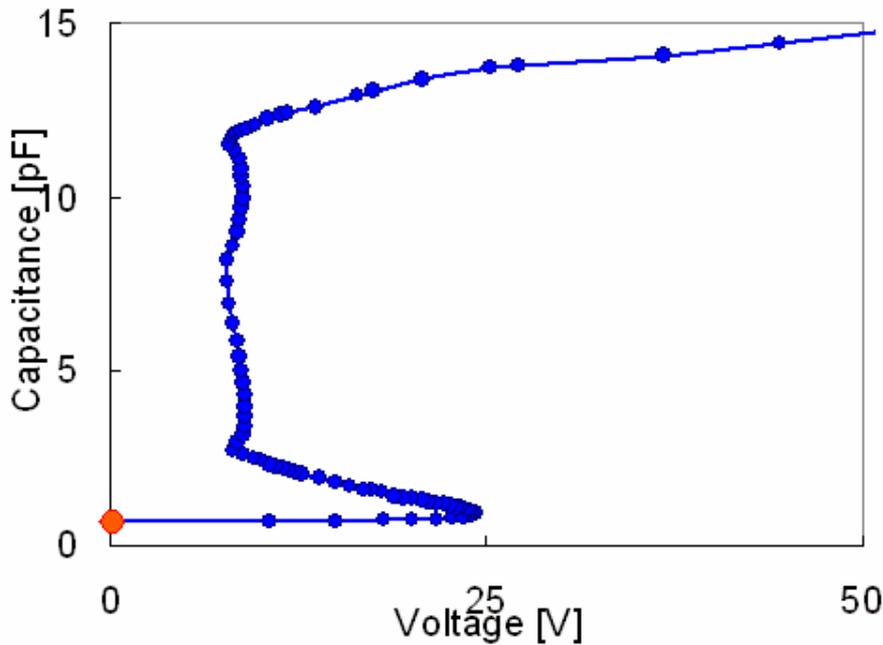


Solving Pull-in instability: DIPIE+

Finite Element implementation DIPIE+ to find static CV-curve:

- Consider every node to prescribe UZ displacement
- Search for voltage for which reaction force vanishes
- Node selection based on largest electrostatic pressure increment

Even better: Numerical continuation

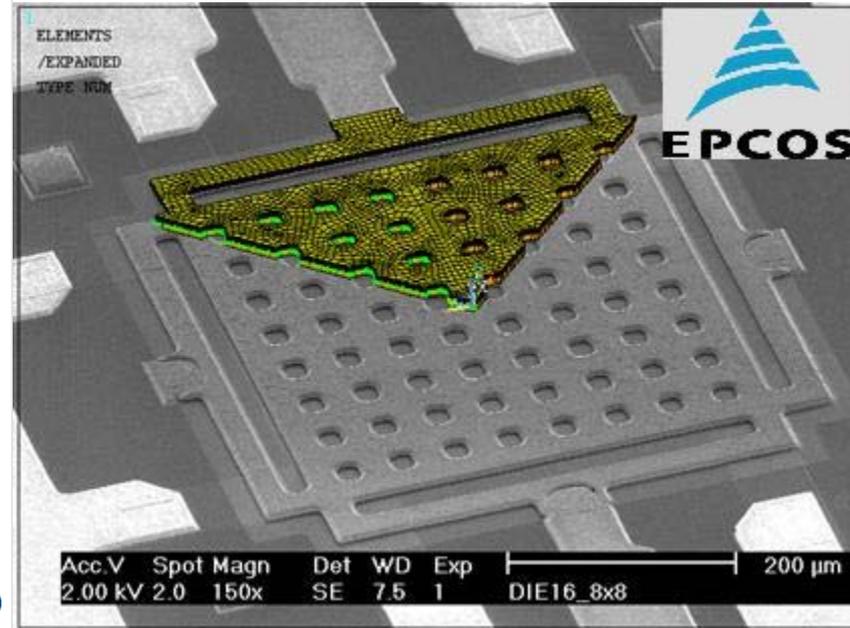
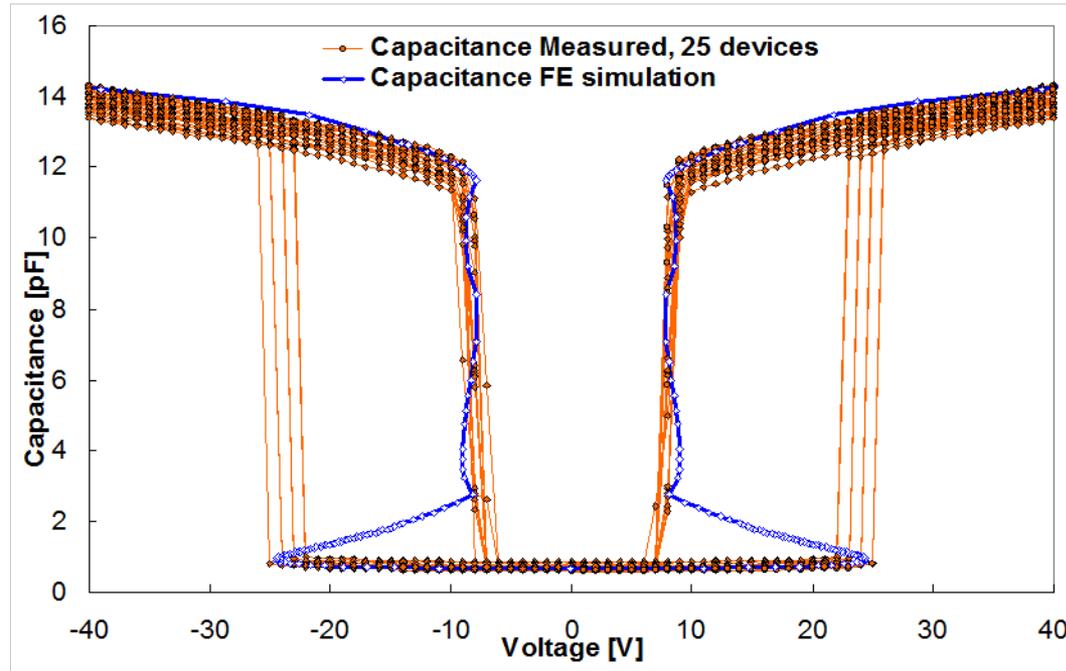


 = prescribed displacement



Multi-physics model: Validation of static solution

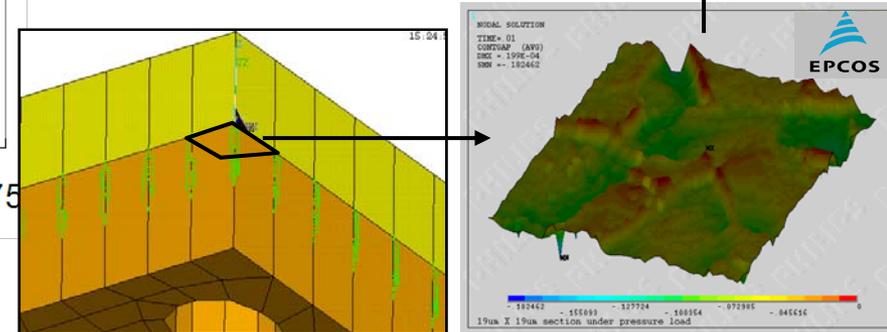
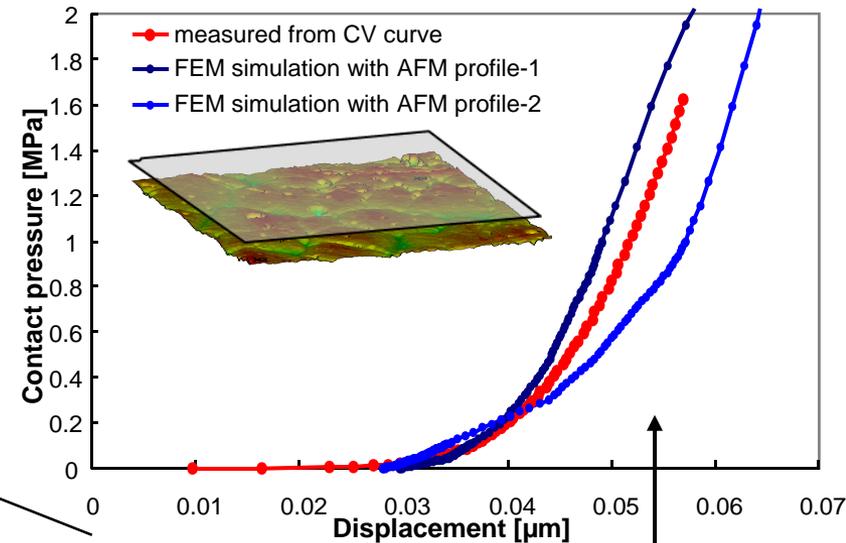
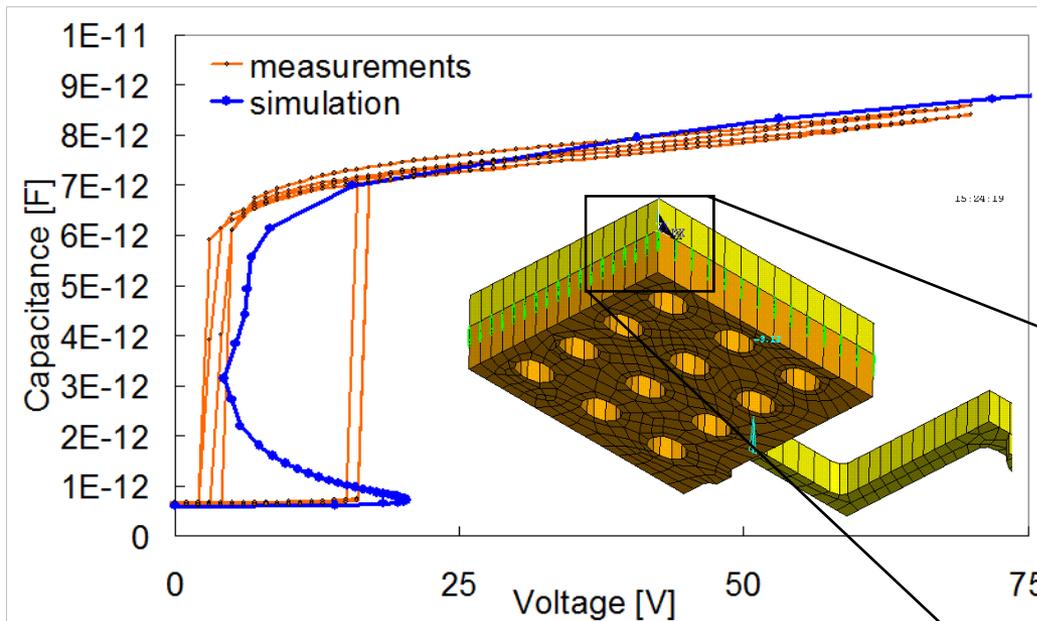
- Good agreement between measured and predicted CV curves
- Slope in closed state capacitance is important feature, caused by surface roughness of the contact



Non-linear Contact model

Surface roughness is homogenized in non-linear contact model:

- Contact behavior pressure(displacement) can be extracted from CV curve
- Simulation of contact pressure-displacement using imported AFM profiles
- Exponential function (I.e. Greenwood model)
- Multi-linear approximation in gasket element



Implementation of new squeeze film element in Ansys:

- structural DOF's added to squeeze film element to create a **directly coupled fluid-structural element**
- Isothermal **non-linear compressible Reynolds equation** (because of large pressure changes when closing):

$$\frac{H}{p} \frac{\partial p}{\partial t} + \frac{\partial H}{\partial t} = \frac{H^3}{p 12 \mu} \left(\left(\frac{\partial p}{\partial x} \right)^2 + \left(\frac{\partial p}{\partial y} \right)^2 \right) + \frac{H^3}{12 \mu} \nabla^2 p$$

- Rarefied gas effects taken into account by an effective viscosity (with optional accommodation factors) as proposed by Veijola:
 - Diffuse reflection:

$$\mu_{eff} = \frac{\mu}{1 + 9.638 \cdot \left(\frac{L0 \cdot P_{L0}}{p \cdot H} \right)^{1.159}}$$

$$Kn = \frac{L0 \cdot P_{L0}}{p \cdot H}$$

H=gap height (=Gap0-UZ) structural DOF

p=Pressure (DOF)

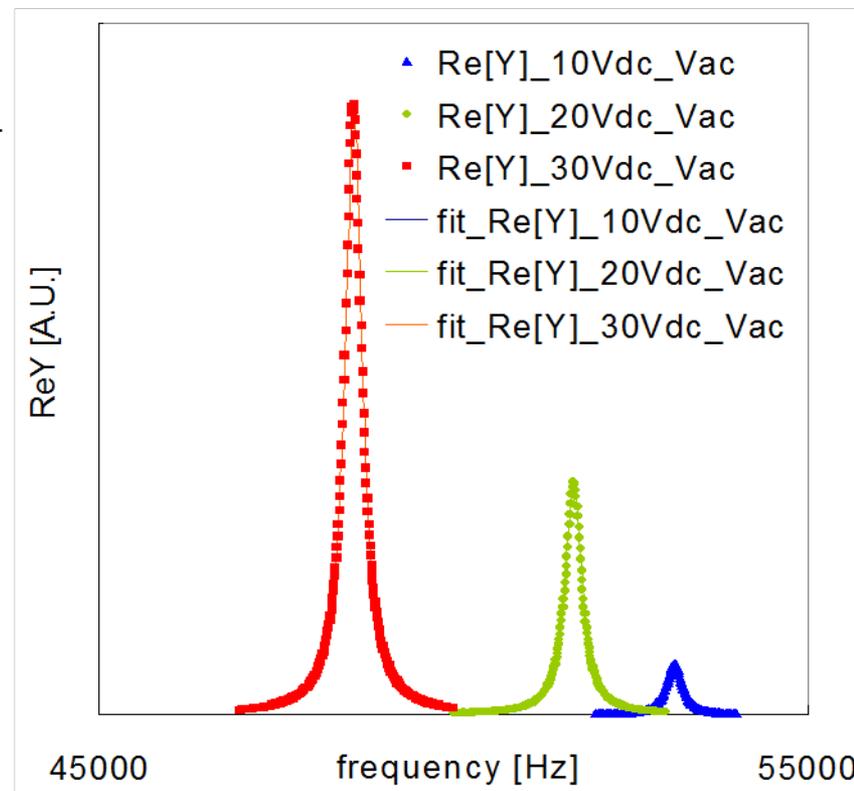
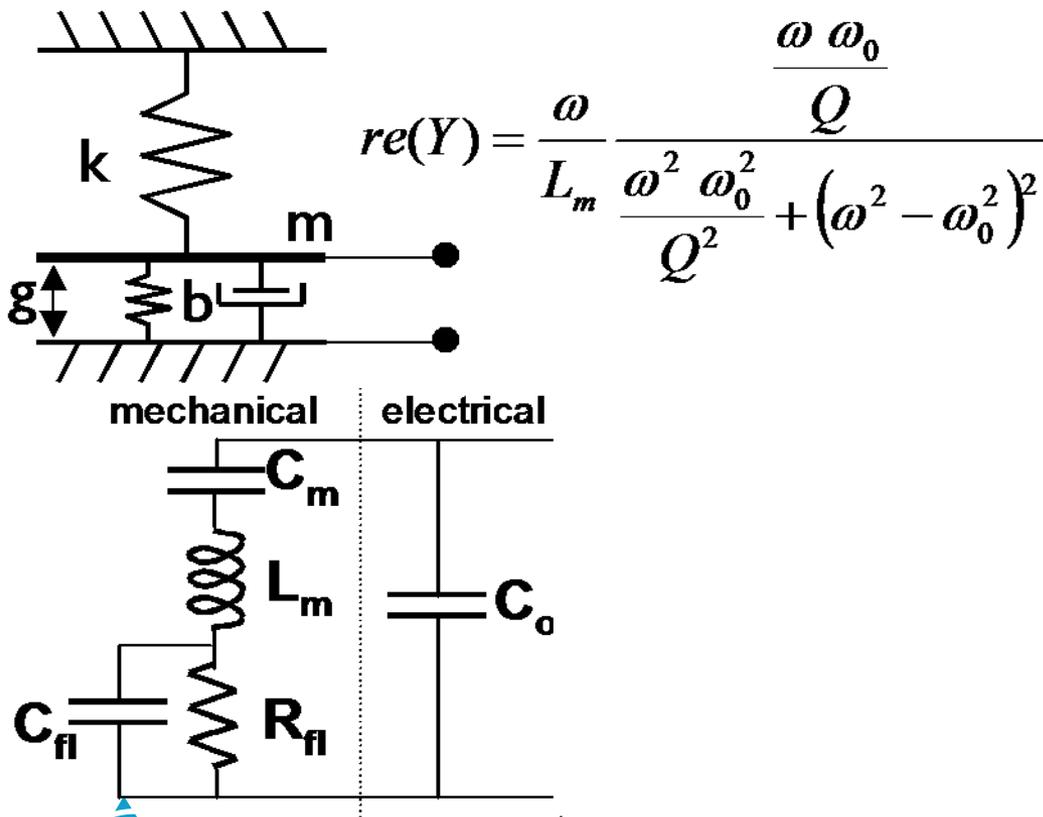
L0=molecular mean free path at P_{L0}

μ=viscosity

Kn= Knudsen number

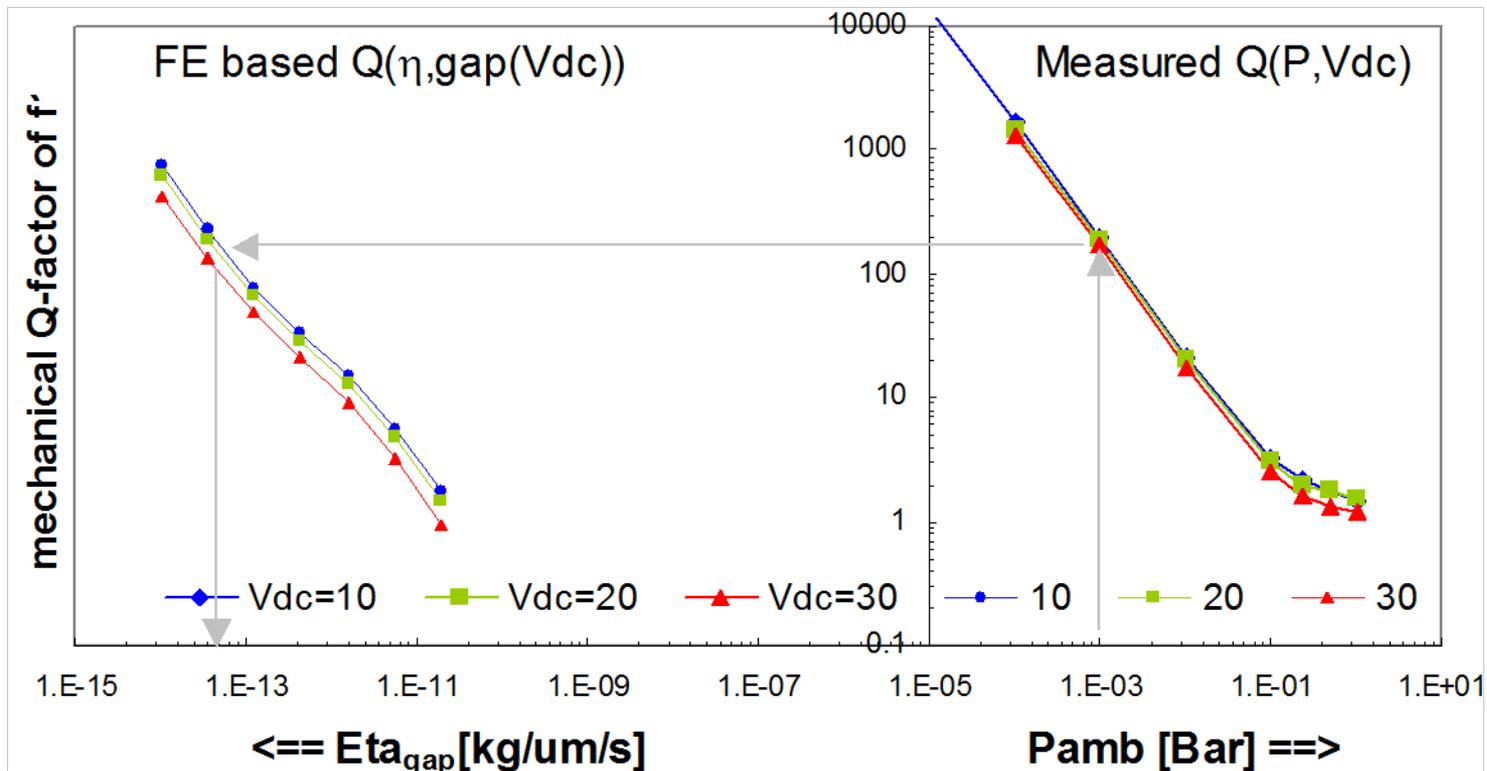
Effective viscosity extracted from measurements

- Impedance analyzer or LCR meter used to measure $\text{Re}[Y]$
- Parasitic shunt branch de-embedded before fitting mechanical Q-factor
- In vacuum chamber to vary ambient pressure



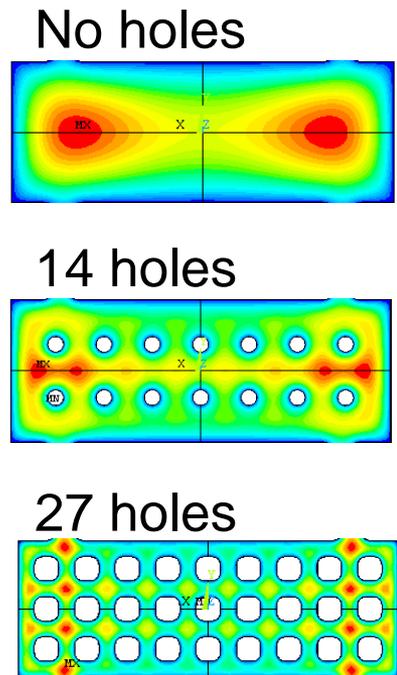
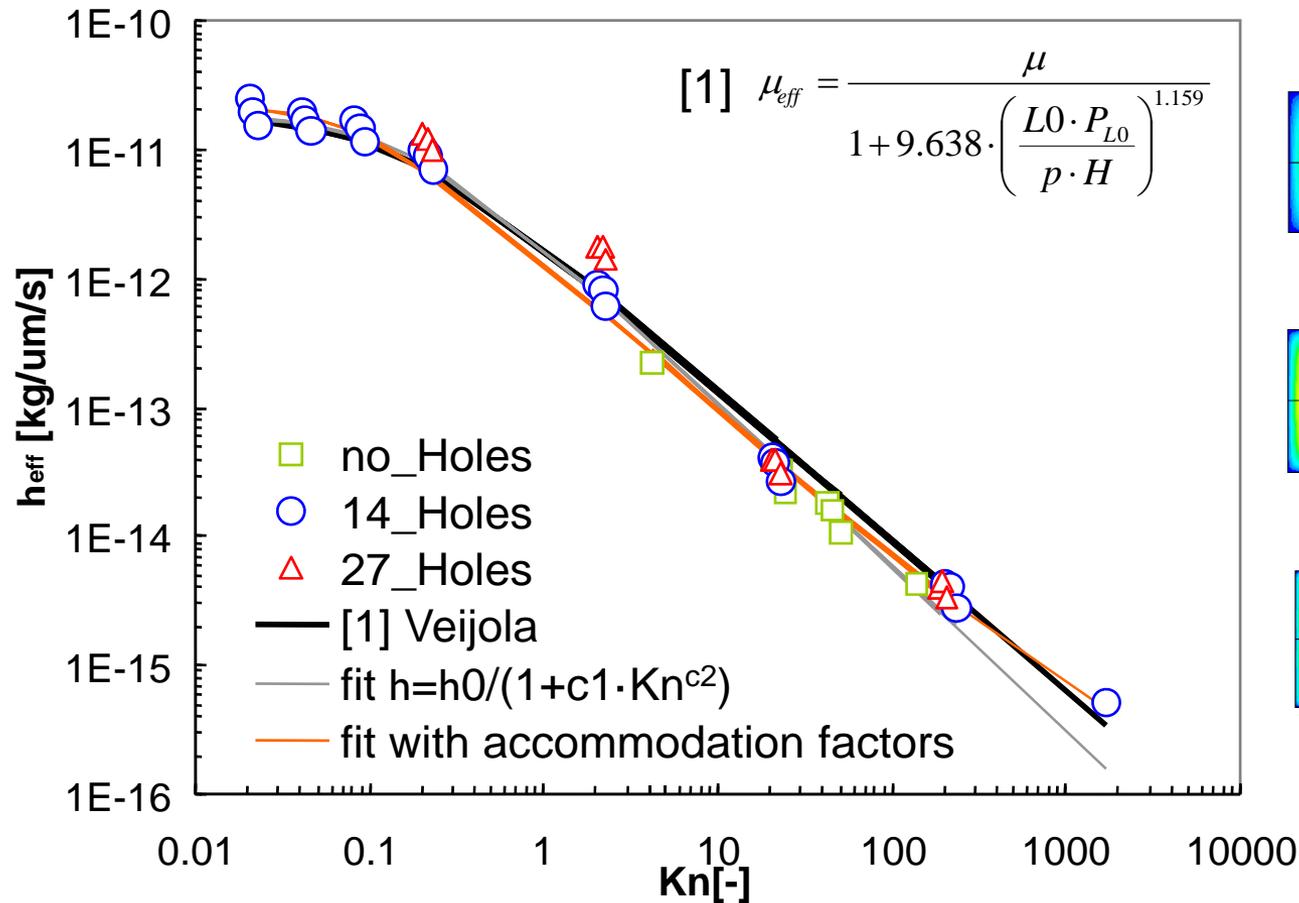
Effective viscosity extracted from measurements

- Measure Q-factor for various designs, bias voltage & pressure range
- Simulate Q-factor's dependency on viscosity & bias voltage
 - Q-factor insensitive to exact match of first eigenfrequency



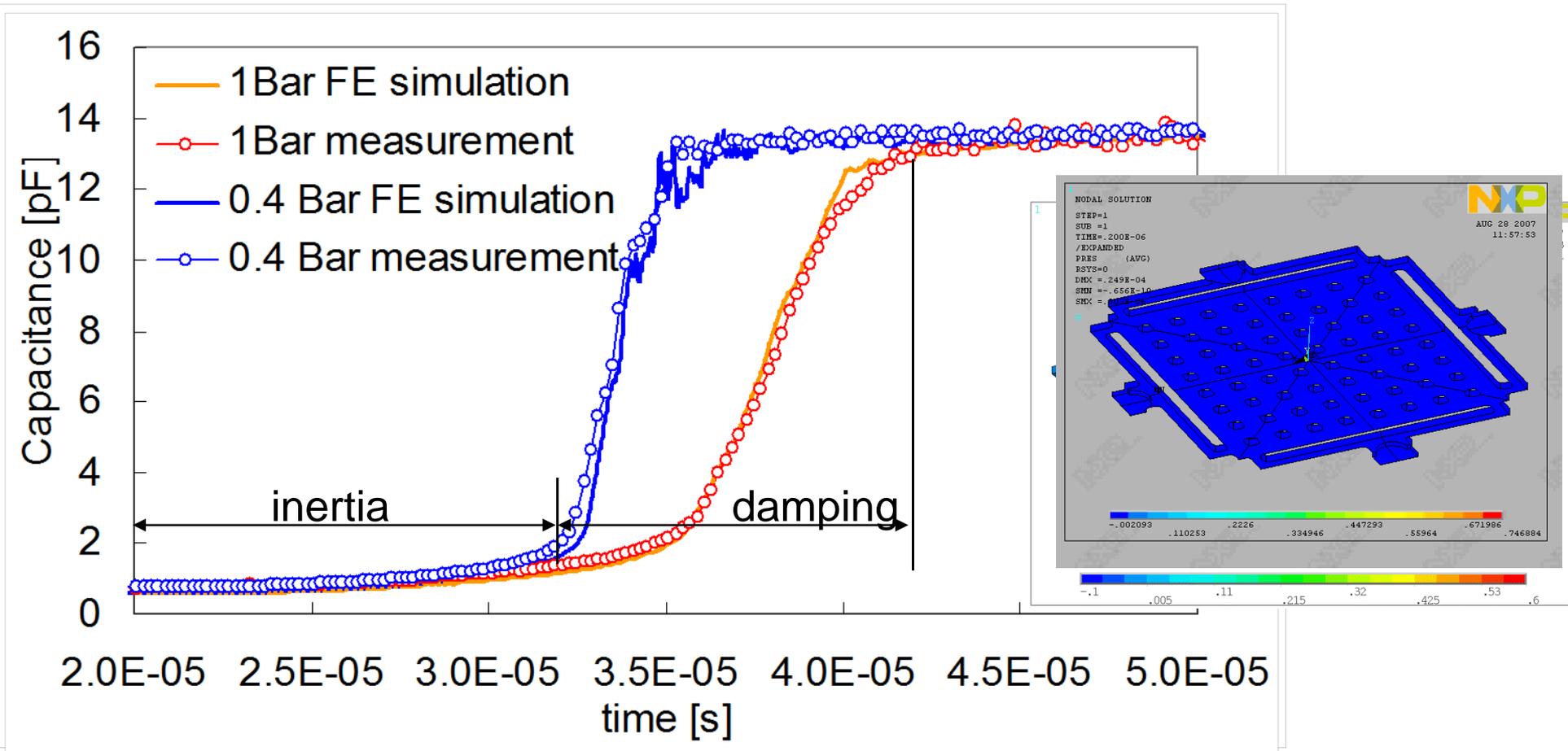
Effective viscosity from measurements

- Small deviation from Veijola
- Better fit obtained by introduction of accommodation factors



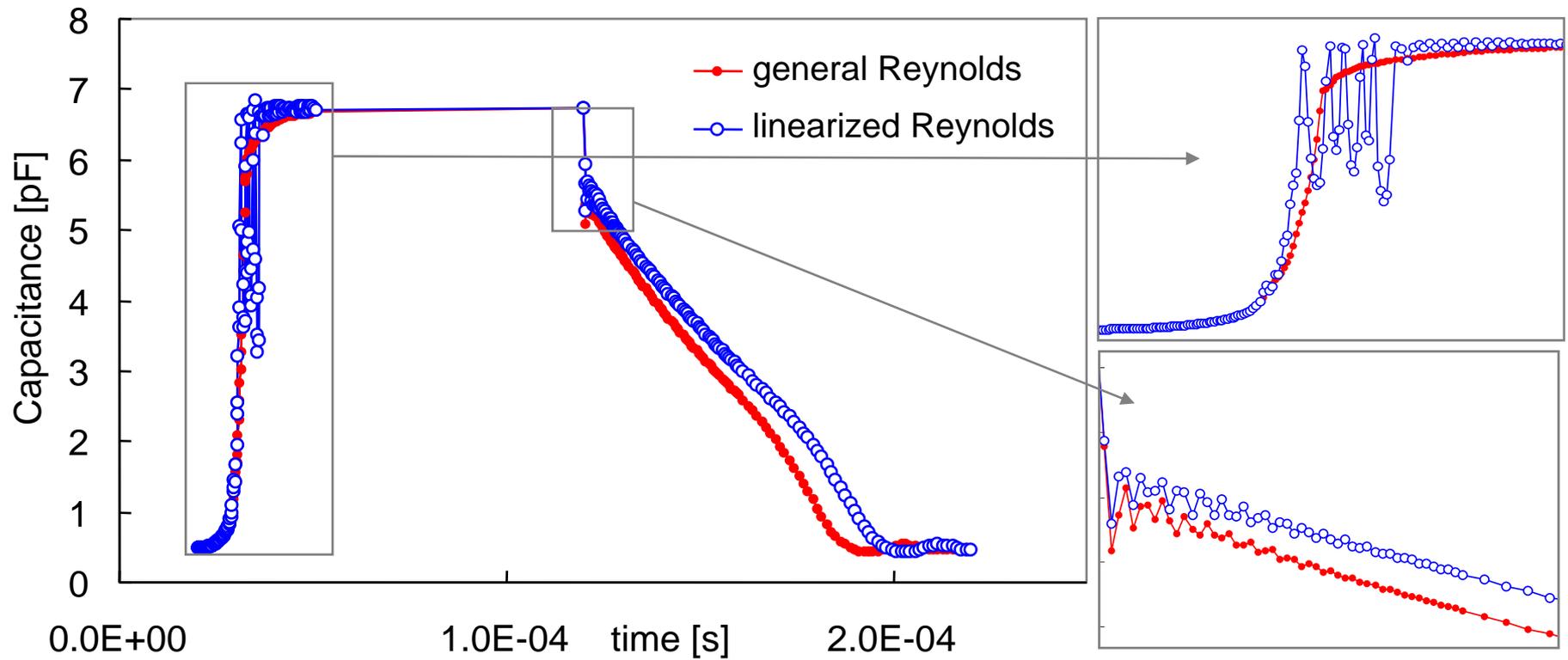
Close/opening transient results

- 8x8 40V open & close transient at 0.4bar & 1bar cavity pressure
- FE model includes initial stress derived from interferometer profiles



Linearized versus general Reynolds equation

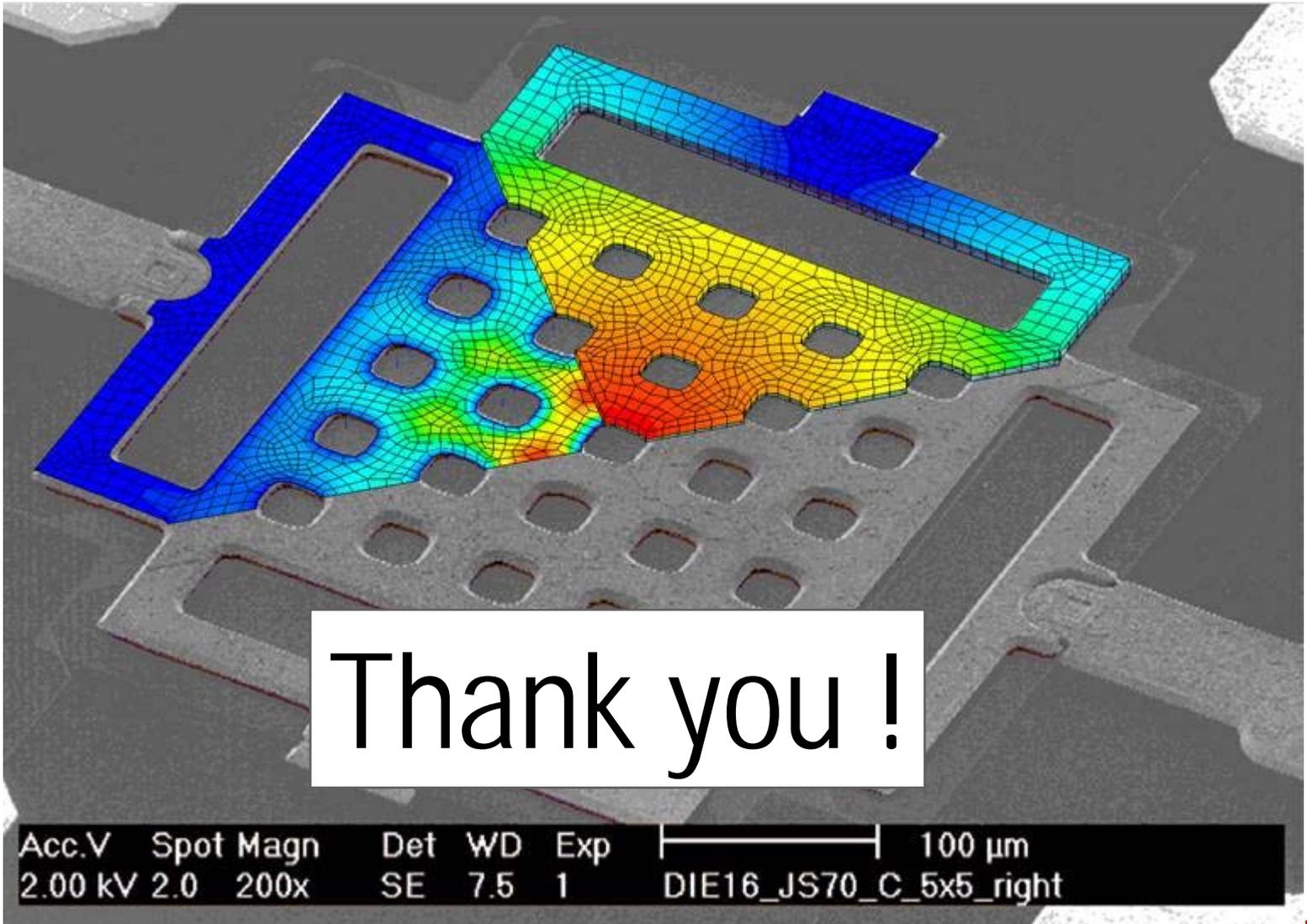
- Significant difference between linearized & non-linear Reynolds
- Pressures clearly outside range for which linearization is valid



- Demonstrated an efficient finite element implementation & validation of squeeze film effects for prediction of transient response
- Rarefaction effects were quantified by extracting the effective viscosity from measurements
- Transient simulations show good agreement with measurements of closing and opening cycles
- Multiphysics simulation improves the design by reducing the opening and closing times for the capacitive switch
- Non-linear Reynolds equation must be used for this type of devices

2020? This is what we'd like to have tomorrow:

- Advanced non-linear multi-physics solver to handle snap-backs:
 - Numerical-continuation e.g. Arc-length for multi-physics
- Non-linear materials in transient with acceptable run-times
 - Multi-size, multi-time scale solution
- More multi-physics domains for reliability assessments:
 - Charge diffusion for dielectric charging (specific for this MEMS)
 - HF-Electro Magnetic to predict power dissipation & temperature
 - Strain gradient crystal plasticity model (adds 18 DOF's) to handle size effects in materials (general for MEMS & NEMS)
- Integration of FE results in system/circuit simulation:
 - Predict large signal system performance (e.g. ACPR) with e.g. harmonic balance



Thank you !

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