



# Modal Analysis in Virtual Prototyping and Product Validation

March 19<sup>th</sup>, 2009





# Agenda

## Modal Analysis in Virtual Prototyping and Product Validation

March 19th, 2009

8am EDT (New York) / 12n GMT (London) / 5:30pm (Bangalore)

### ▲ Welcome & Introduction (Overview of NAFEMS Activities)

▲ Mr. David Quinn, *NAFEMS Marketing and Communications*

### ▲ Modal Analysis in Virtual Prototyping and Product Validation

▲ Mr. Dhanushkodi D.M., *TechPassion Technologies Pvt. Ltd.*

### ▲ Q&A Session

▲ Panel

### ▲ Closing



Quinn



Dhanushkodi



THE INTERNATIONAL ASSOCIATION  
FOR THE ENGINEERING ANALYSIS  
COMMUNITY

# An Overview of NAFEMS Activities



David Quinn  
NAFEMS  
Marketing & Communications



# Planned Activities

## ➤ Webinars

- New topic each month!
  - March 19<sup>th</sup> - Modal Analysis in Virtual Prototyping and Product Validation
- Recent webinars:
  - Pathways to Future CAE Technologies and their Role in Ambient Intelligent Environments
  - Computational Structural Acoustics: Technology, Trends and Challenges
  - FAM: Advances in Research and Industrial Application of Experimental Mechanics
  - CCOPPS: Power Generation: Engineering Challenges of a Low Carbon Future
  - Practical CFD Analysis
  - Complexity Management
  - CCOPPS: Creep Loading of Pressurized Components – Phenomena and Evaluation
  - Multiphysics Simulation using Implicit Sequential Coupling
  - CCOPPS: Fatigue of Welded Pressure Vessels
  - Applied Element Method as a Practical Tool for Progressive Collapse Analysis of Structures
  - AUTOSIM: The Future of Simulation in the Automotive Industry
  - A Common Sense Approach to Stress Analysis and Finite Element Modeling
  - The Interfacing of FEA with Pressure Vessel Design Codes (CCOPPS Project)
  - Multiphysics Simulation using Directly Coupled-Field Element Technology
  - Methods and Technology for the Analysis of Composite Materials
  - Simulation Process Management
  - Simulation-supported Decision Making (Stochastics)
  - Simulation Driven Design (SDD) Findings

**To register for upcoming webinars, or to view a past webinar,  
please visit: [www.nafems.org/events/webinars](http://www.nafems.org/events/webinars)**



- ▲ Establishes in 2009
- ▲ Proposed initial course offerings:
  - ▲ Dynamic FE Analysis
  - ▲ Stochastics
  - ▲ Composites
  - ▲ Verification & Validation
- ▲ Next course:
  - ▲ Topic: Dynamic FE Analysis
  - ▲ Start: April 21<sup>st</sup>, 2009 (six-week course)
- ▲ For more information, visit: [www.nafems.org/e-learning](http://www.nafems.org/e-learning)



▲ When: June 16<sup>th</sup> – 19<sup>th</sup>, 2009

▲ Where: Crete, Greece

▲ Updates:

▲ Over 200 presentations

▲ Six Keynote Presentations

▲ Additional Workshops and Activities:

▲ Mini-symposium: Analysis and Simulation of Composite Structures Including Damage and Failure Prediction

▲ Engineering Analysis Quality, Verification & Validation



## ▲ Additional Workshops and Activities (cont.):

- ▲ High Performance Computing in Engineering Simulation
- ▲ Multi-physics Simulation: Advanced Coupling Algorithms and Strategies
- ▲ Crash



## ► Additional Workshops and Activities (cont.):

- EC AUTOSIM Project – (one year)
- EC FENet Project – (four years)
- EC Multi-Scale Analysis of Large Aerostructures Project
- NAFEMS Skills Management Initiative
- Simulation Data Management
- Material Data
- Optimization/Robustness/Stochastics
- Round Table Discussion on Business Drivers



# NWC 2009

NAFEMS WORLD CONGRESS 09  
JUNE 16th - 19th      CRETE - GREECE

## NWC09 Keynotes

➤ **Erich Schelkle** - Porsche AG and Automotive Simulation Center Stuttgart, Germany



➤ **Tsuyoshi Yasuki** - Toyota Motor Corporation, Japan



➤ **Martin Wiedemann** - DLR German Aerospace Center, Germany



➤ **Jacek Marczyk** - Ontonix, Italy



➤ **Louis Komzsik** - Siemens PLM Software, USA



➤ **François Besnier** - Principia RD, France





# NWC 2009

NAFEMS WORLD CONGRESS 09  
JUNE 16<sup>th</sup> - 19<sup>th</sup> CRETE - GREECE

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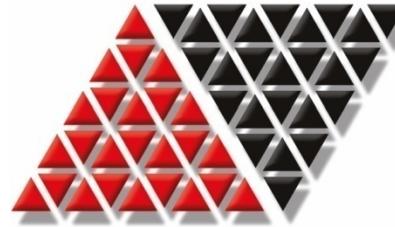
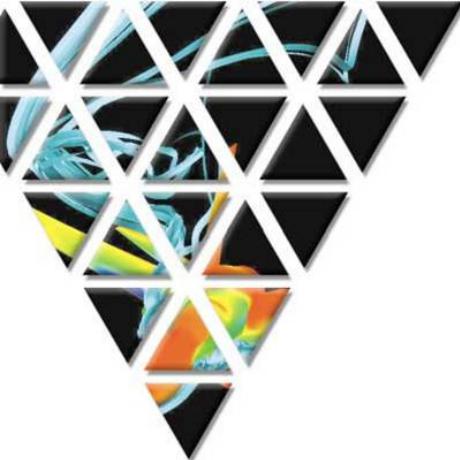


► For more information about the NWC09, please visit: [www.nafems.org/congress](http://www.nafems.org/congress).

► Sponsorship and Exhibition Opportunities Still Available!

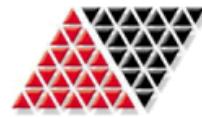
► For more information, please visit:  
[www.nafems.org/congress/sponsor](http://www.nafems.org/congress/sponsor).





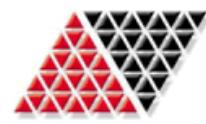
# Modal Analysis in Virtual Prototyping and Product Validation



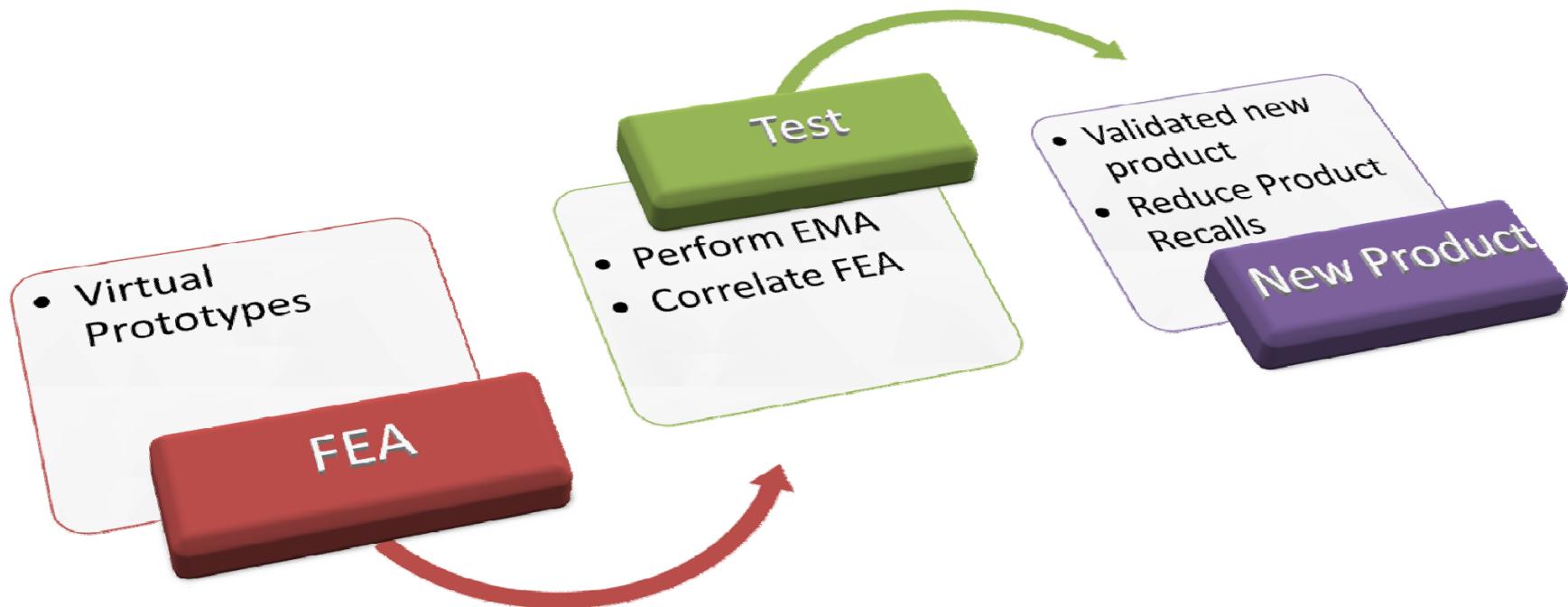


# Outline

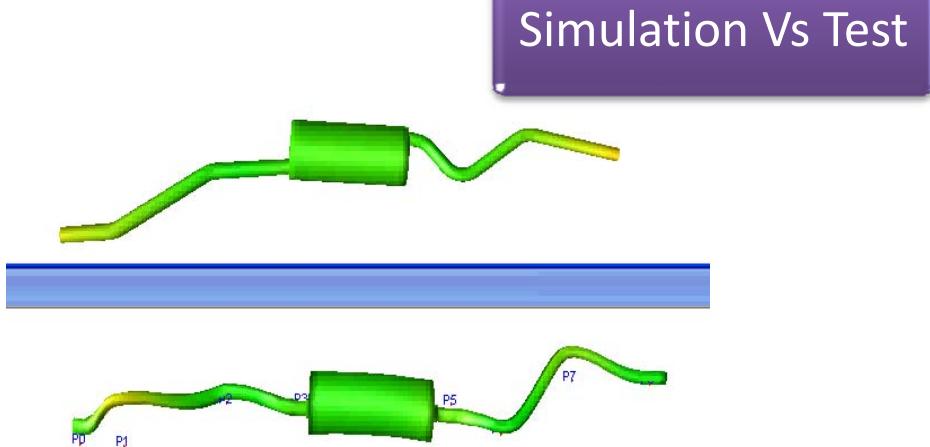
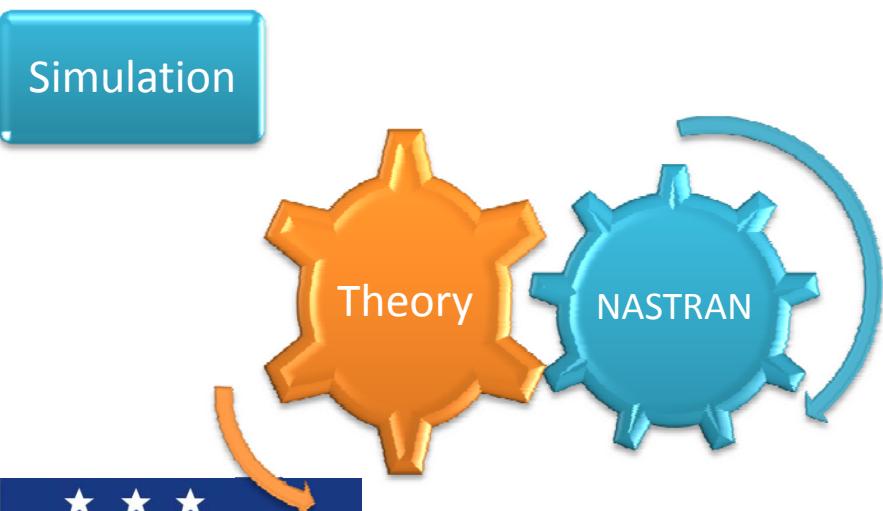
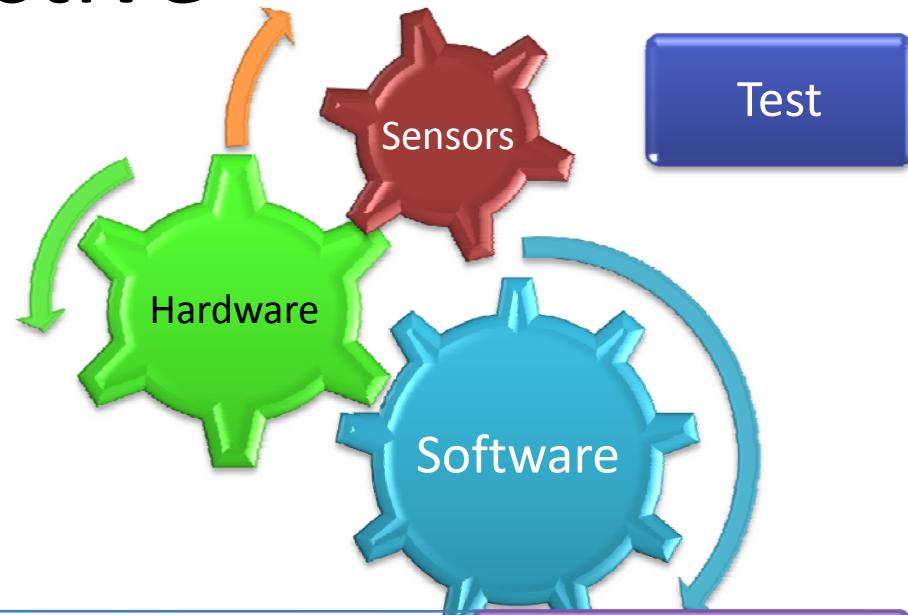
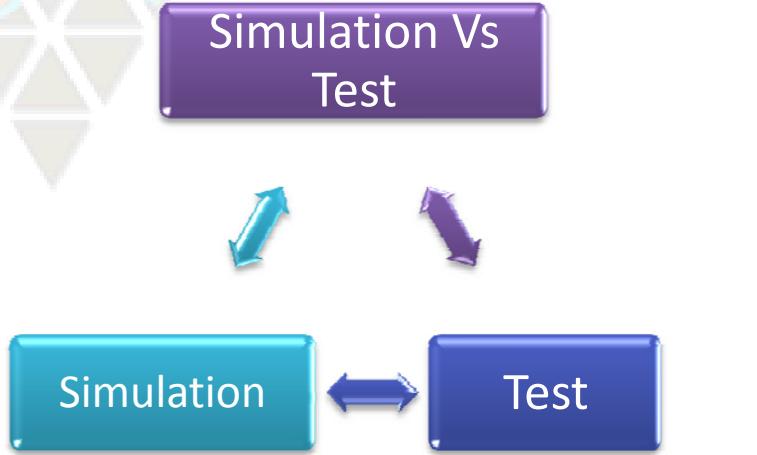
1. Finite Element Analysis
  1. Modal Parameters
  2. Damping Estimation
2. Experimental Modal Analysis
  1. Input – Output Modal Analysis
  2. Operational Modal Analysis
  3. Experimental Setup
  4. Modal Parameter Extraction
  5. Time Domain Methods
  6. Frequency Domain Methods
3. Correlation
  1. Qualitative : Visual Correlation
  2. Quantitative : Numerical Correlation
4. Case Studies
  1. Exhaust Pipe : Determining parameters using experimental modal analysis
  2. Determination of Damping : Connecting Rod, Exhaust pipe



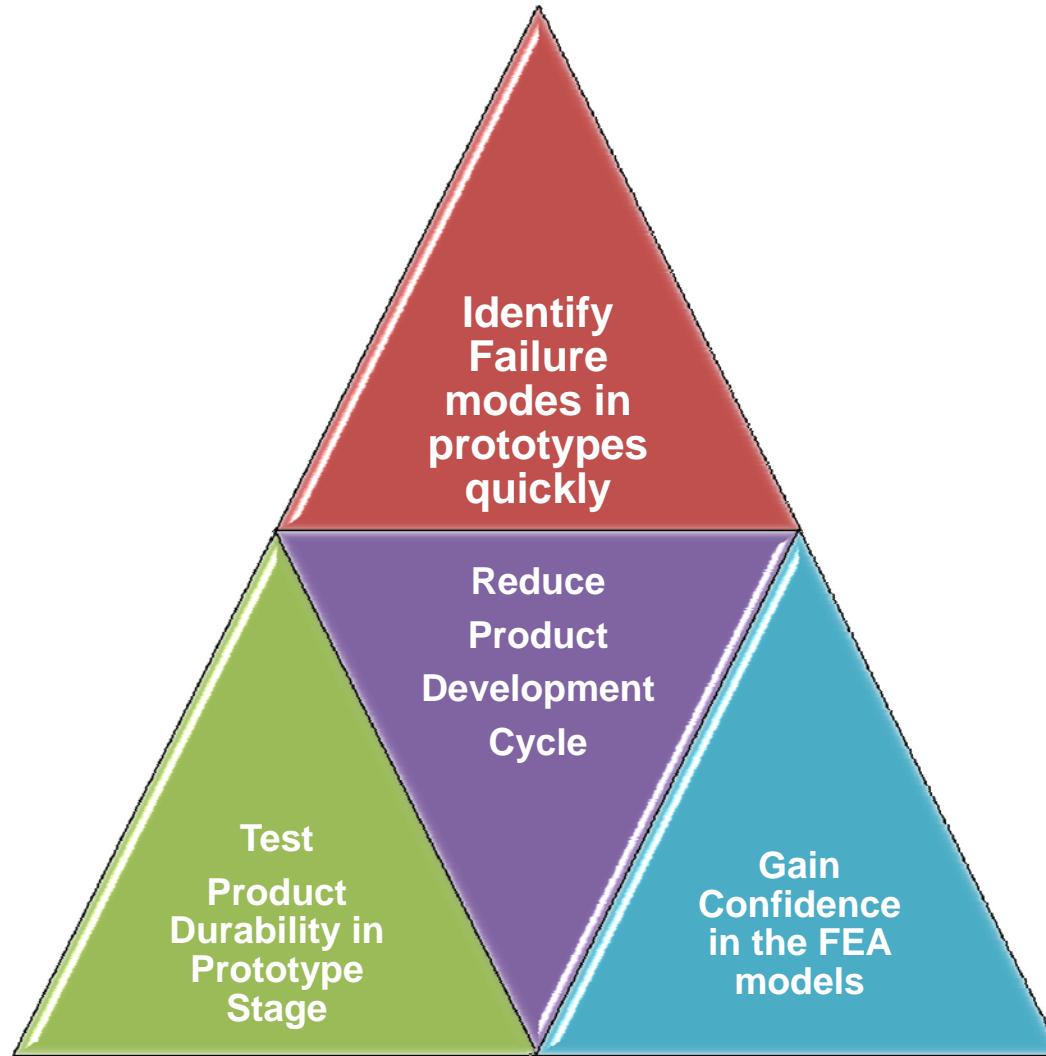
# Product Development Stages

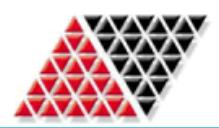
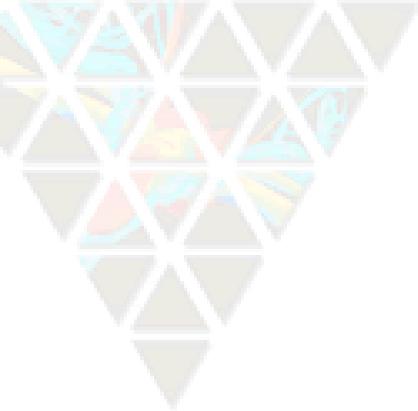


# Perspective



# Realizable Benefits





Simulation

# The Finite Element Approach

# Finite element methodology

## The basic concept

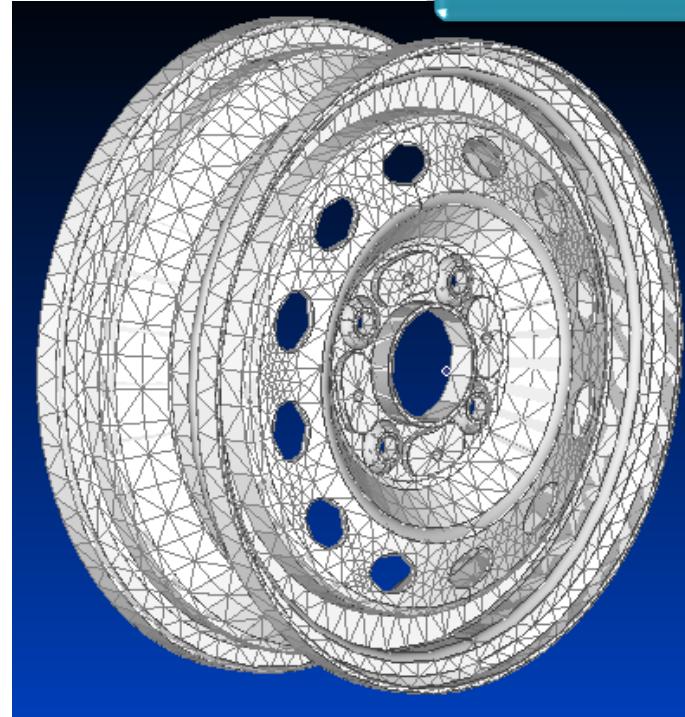
Simulation

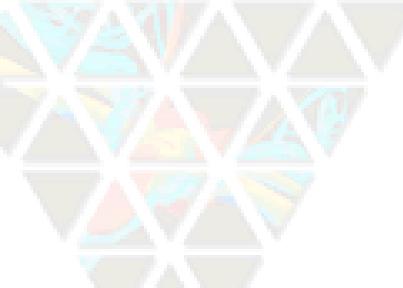


CAD



Mesh Model





# Finite element methodology

## Steps involved



Simulation

Step 1

- Descretization

Step 2

- Shape Functions

Step 3

- Element Matrices

Step 4

$$\det([K] - \omega^2[M]) = 0$$

Step 5

- Natural Frequencies and Modeshapes

# The Modal Problem - Formulation



Simulation

$$[M] \frac{(d^2 \vec{Q})}{(dt^2)} + [C] \frac{(d \vec{Q})}{(dt)} + [K] \vec{Q} = \vec{P}$$

---

$$[M^{(e)}] = [\lambda]^T [m^{(e)}] [\lambda] \quad [K^{(e)}] = \iiint_{V^{(e)}} [B]^T [D] [B]. dv$$

$$[m^{(e)}] = \iiint_{V^{(e)}} \rho [N]^T [N]. dv \quad [C^{(e)}] = \iiint_{V^{(e)}} \mu [N]^T [N]. dv$$

---

$$\det [[K] - \omega^2 [M]] = 0$$



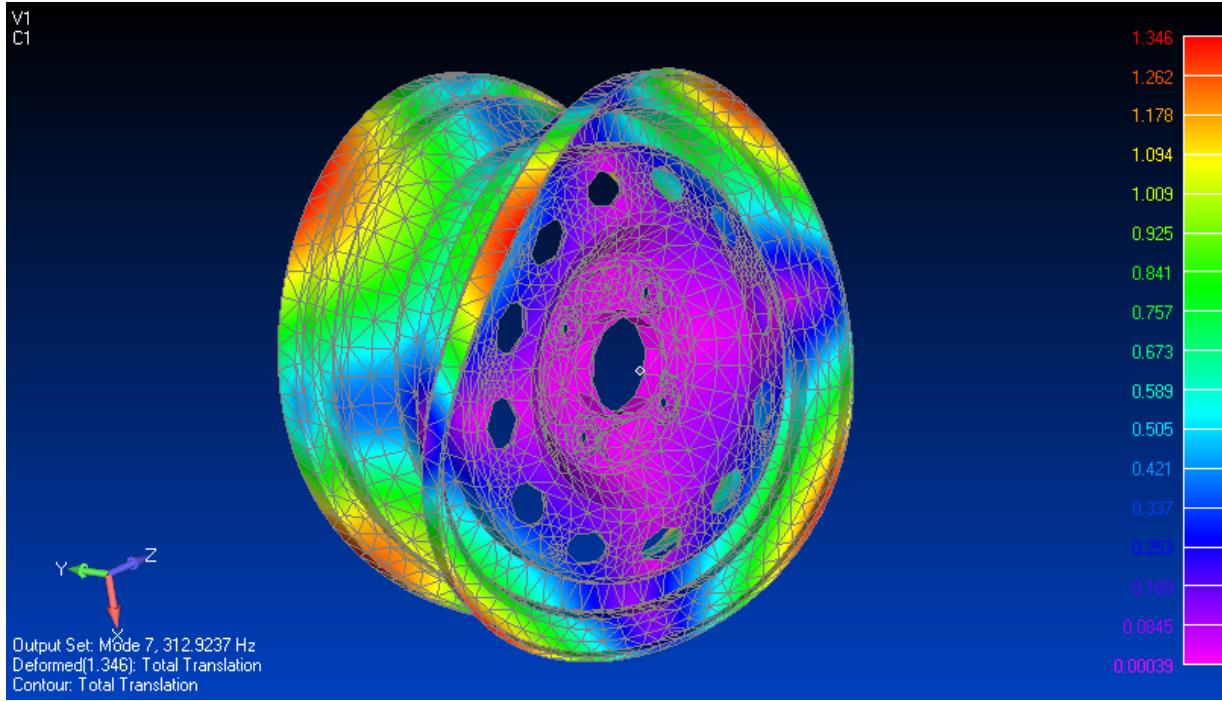
# Finite element solving



Simulation



# Post Processing



Simulation

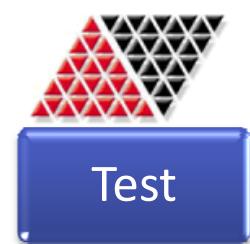
- Results**
- 1..Mode 1, 0.001619 Hz
  - 2..Mode 2, 0.00106144 Hz
  - 3..Mode 3, 7.25843E-4 Hz
  - 4..Mode 4, 5.72727E-4 Hz
  - 5..Mode 5, 9.43343E-4 Hz
  - 6..Mode 6, 0.00124043 Hz
  - 7..Mode 7, 312.9237 Hz
  - 8..Mode 8, 313.3075 Hz
  - 9..Mode 9, 893.8043 Hz
  - 10..Mode 10, 894.4085 Hz
  - 11..Mode 11, 942.1146 Hz
  - 12..Mode 12, 1240.738 Hz
  - 13..Mode 13, 1243.269 Hz
  - 14..Mode 14, 1271.967 Hz
  - 15..Mode 15, 1274.79 Hz
  - 16..Mode 16, 1499.329 Hz
  - 17..Mode 17, 1502.604 Hz
  - 18..Mode 18, 1525.914 Hz
  - 19..Mode 19, 1527.325 Hz
  - 20..Mode 20, 1605.13 Hz

At each of the mode that is solved for, we can obtain the natural frequency and the respective deflection shape – Mode Shape



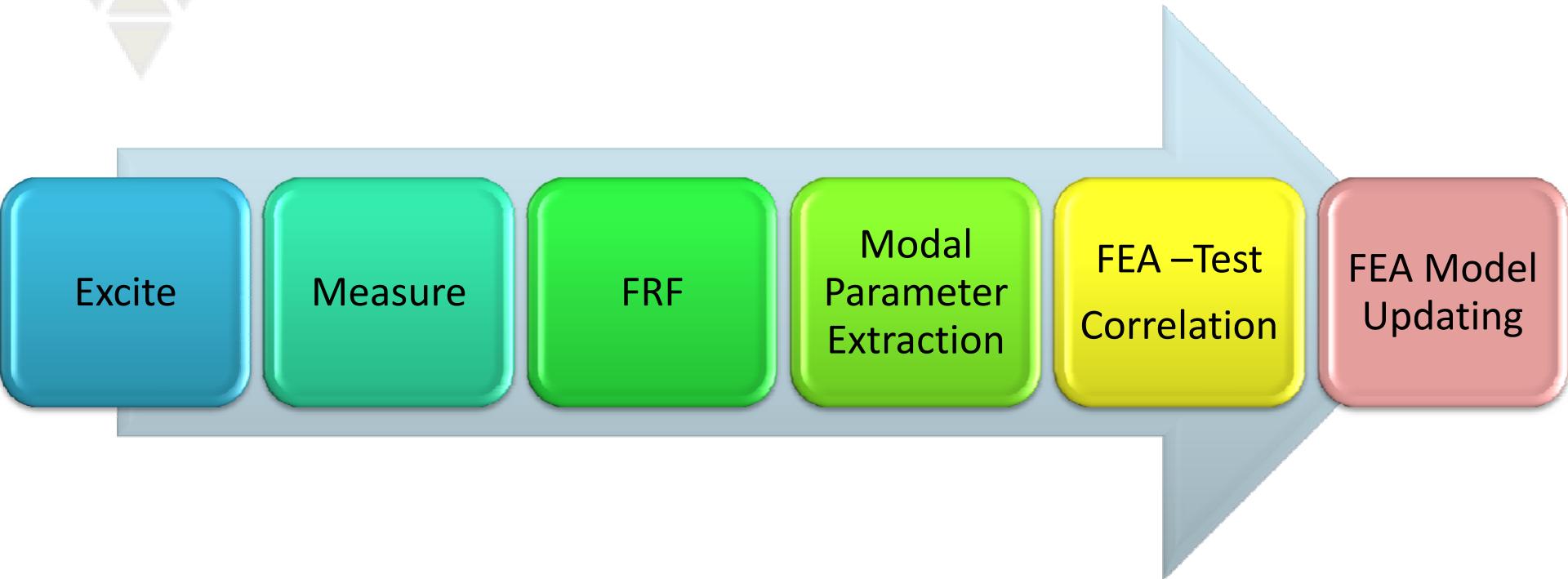
Simulation

# Experimental Modal Analysis

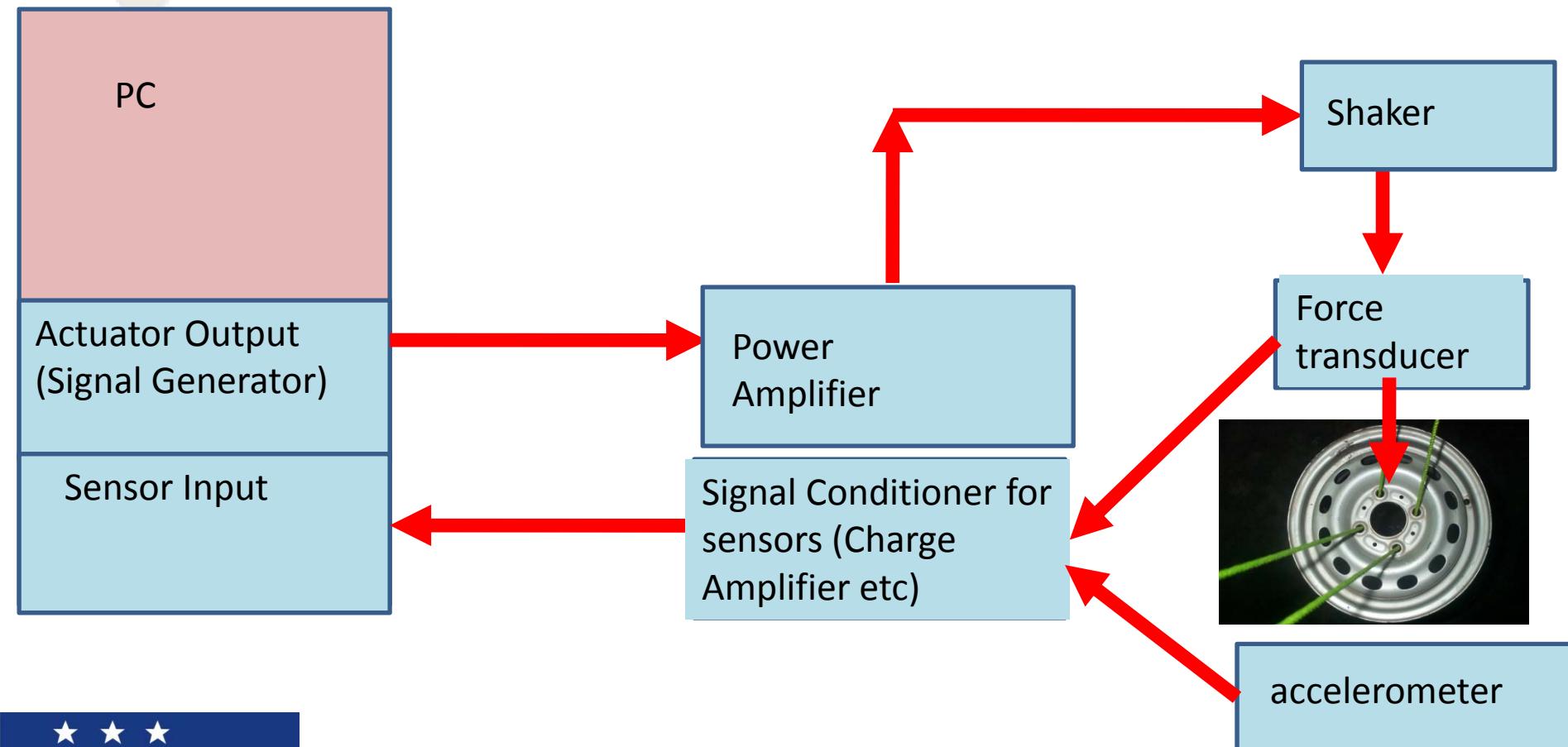


Test

# Overview

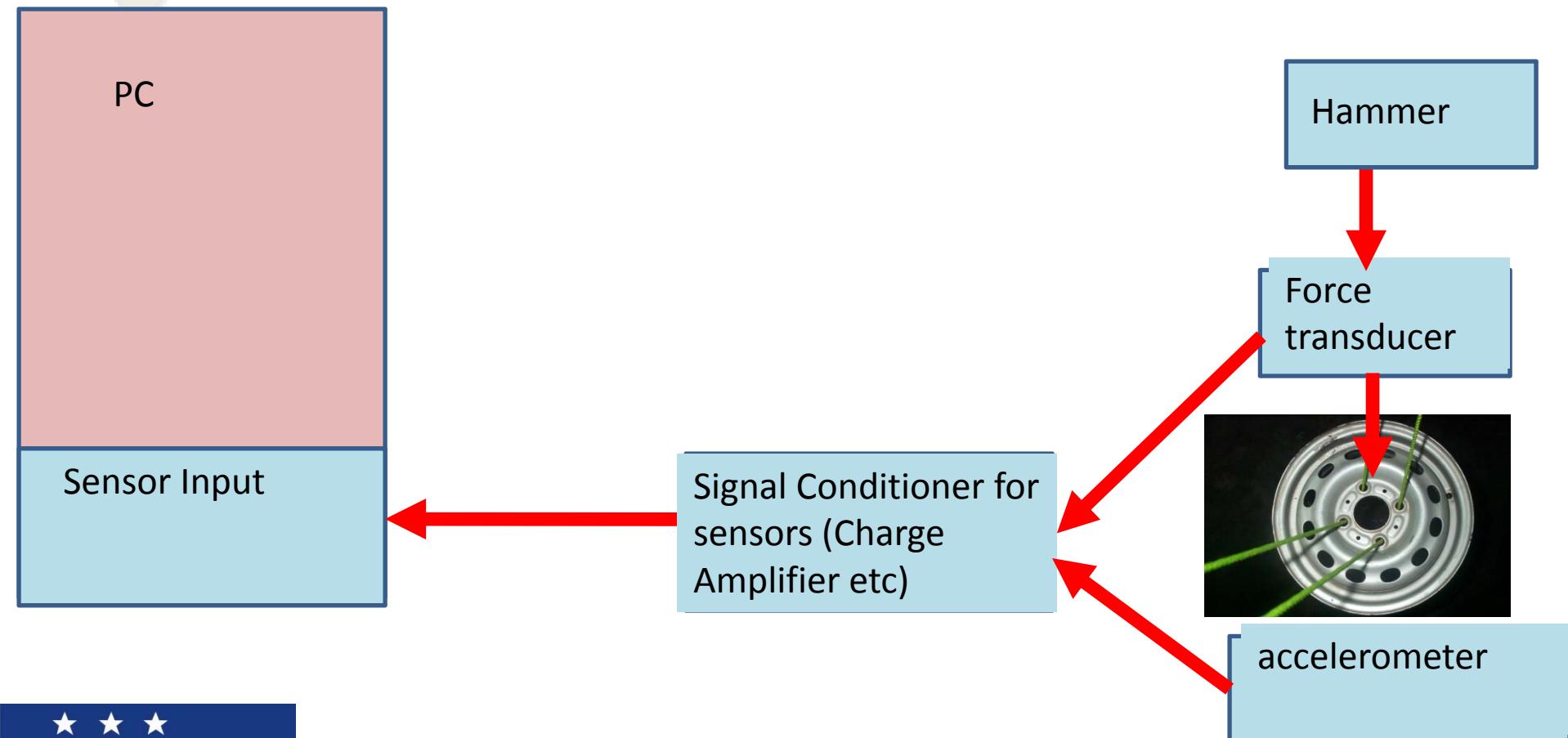


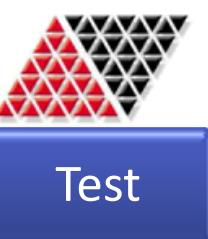
# Experimental Setup-1



# Experimental Setup-2

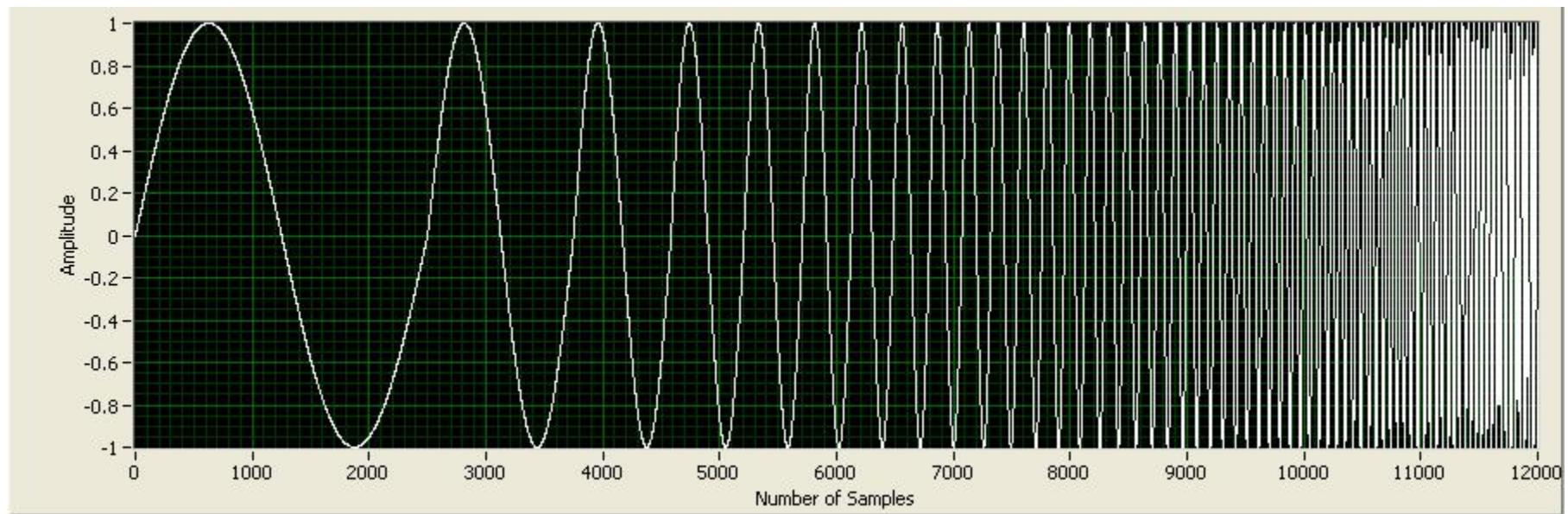
Test

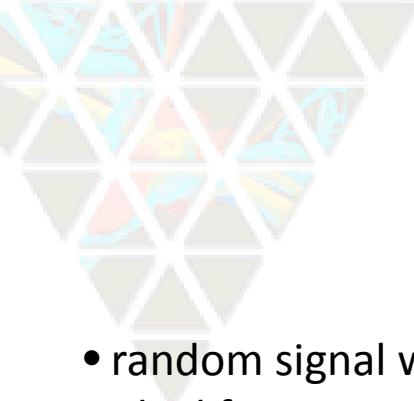




# Sinusoidal Excitation

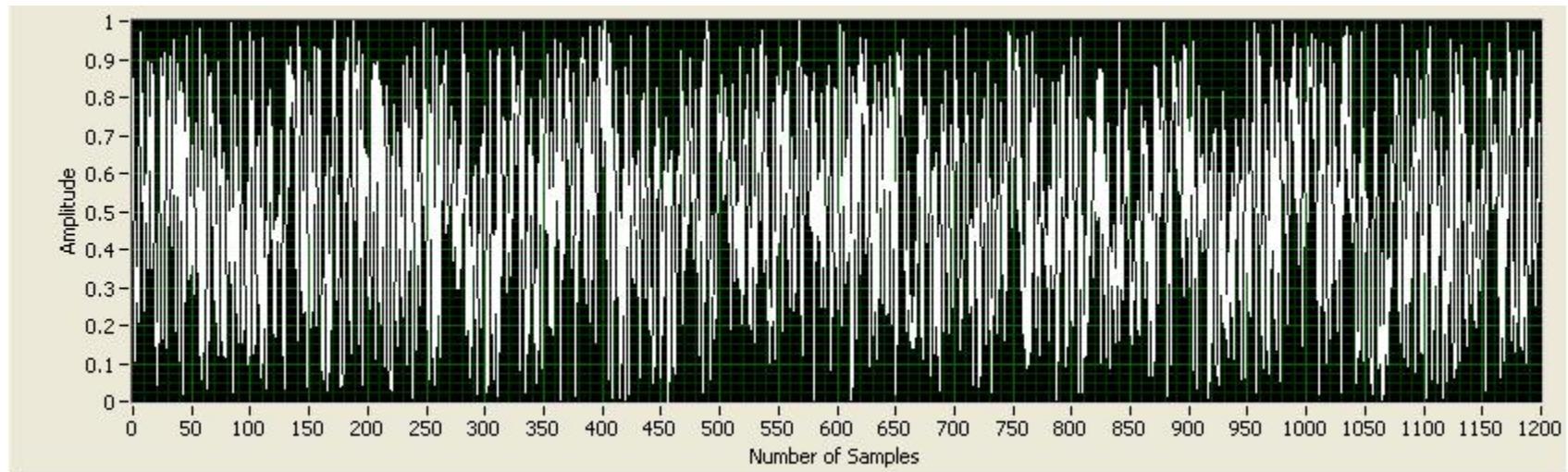
- Sweep from a low frequency to high frequency in steps
- Ideal for structures with non-linearity and are highly damped

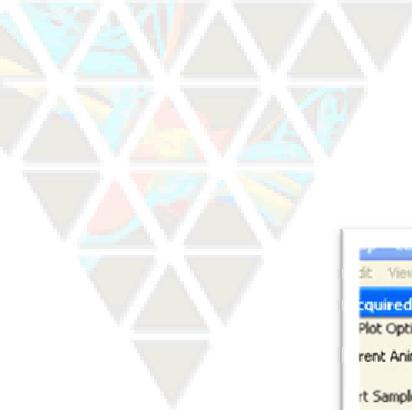




# Random Excitation

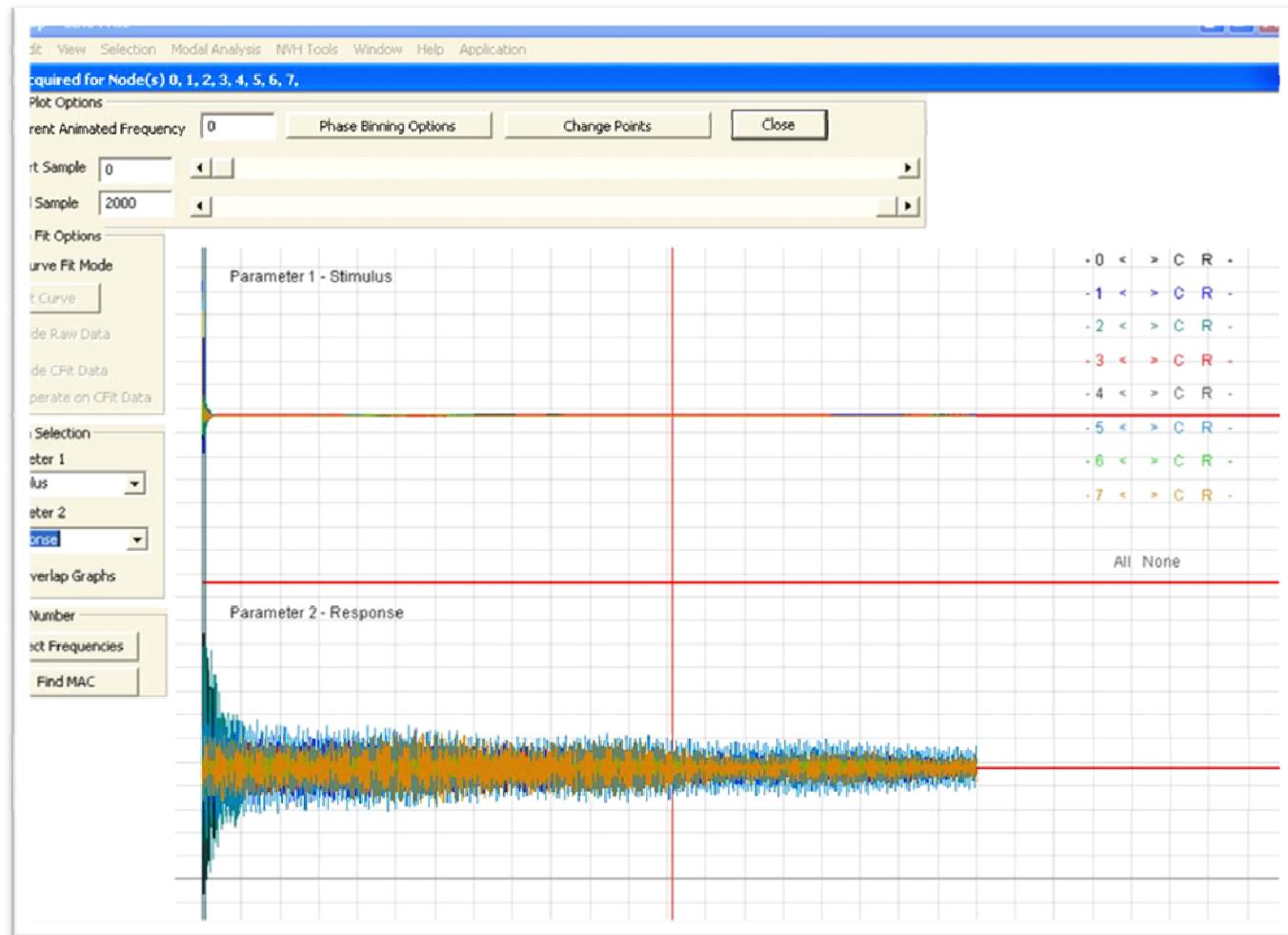
- random signal with Gaussian distribution
- Ideal for structures with non-linearity
- Leakage exists as the force and response signals are non-periodic

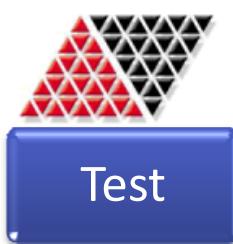




Test

# Impact Excitation





# Excite - Measure





# Frequency Response Function

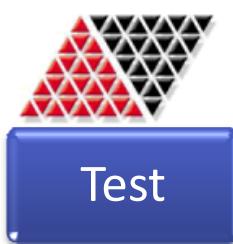
## FRF

$$\text{Receptance} = \frac{\text{Displacement}}{\text{Force}}$$

$$H(\omega) = \frac{Y(\omega)}{X(\omega)}$$

$$\text{Mobility} = \frac{\text{Velocity}}{\text{Force}}$$

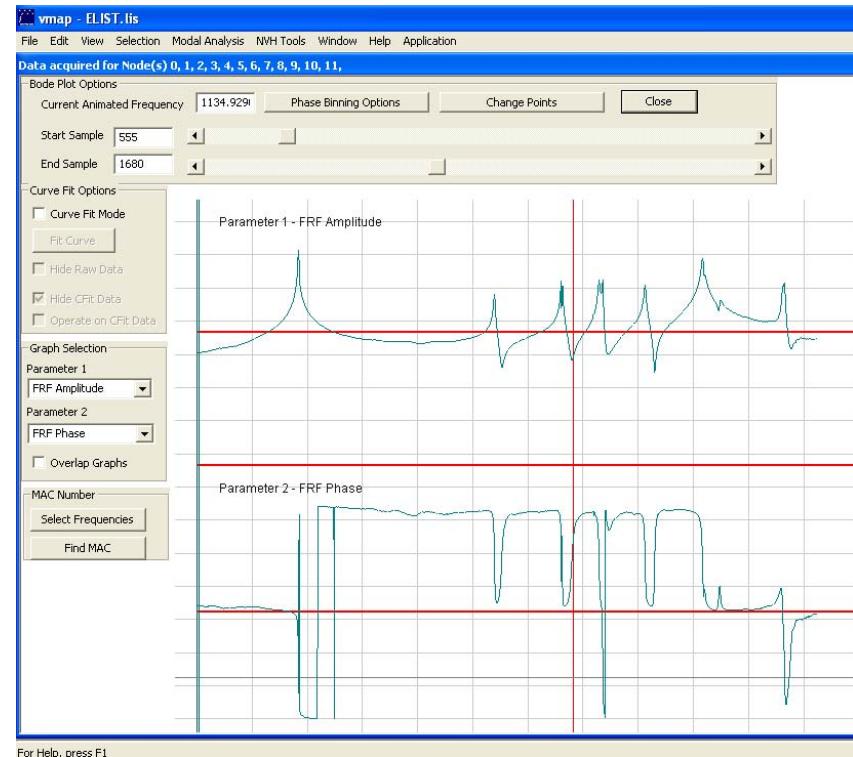
$$\text{Accelerance} = \frac{\text{Acceleration}}{\text{Force}}$$



# FRF Estimators

- Noise level in excitation and response determines the accuracy
- Near resonance, response noise can be ignored
- Near anti-resonance, excitation noise can be ignored

$$H(\omega) = \frac{Y(\omega)}{X(\omega)}$$



One FRF estimator does not fit all situations



# Linearity

- Modal Analysis is meaningless without the assumption of linearity

## Linearity Test

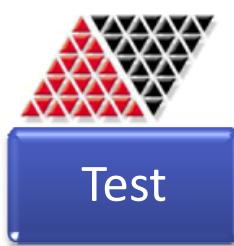
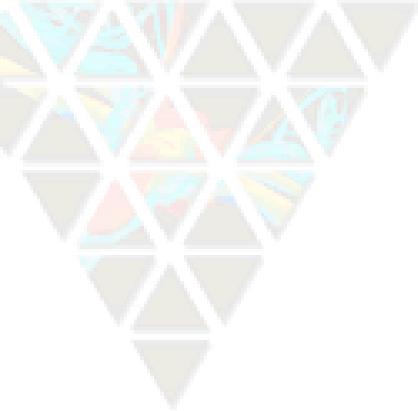
FRF must be independent of excitation amplitudes

# Reciprocity

A LTI (Linear Time-Invariant) System follows reciprocity



$$H_{12} = H_{21}$$



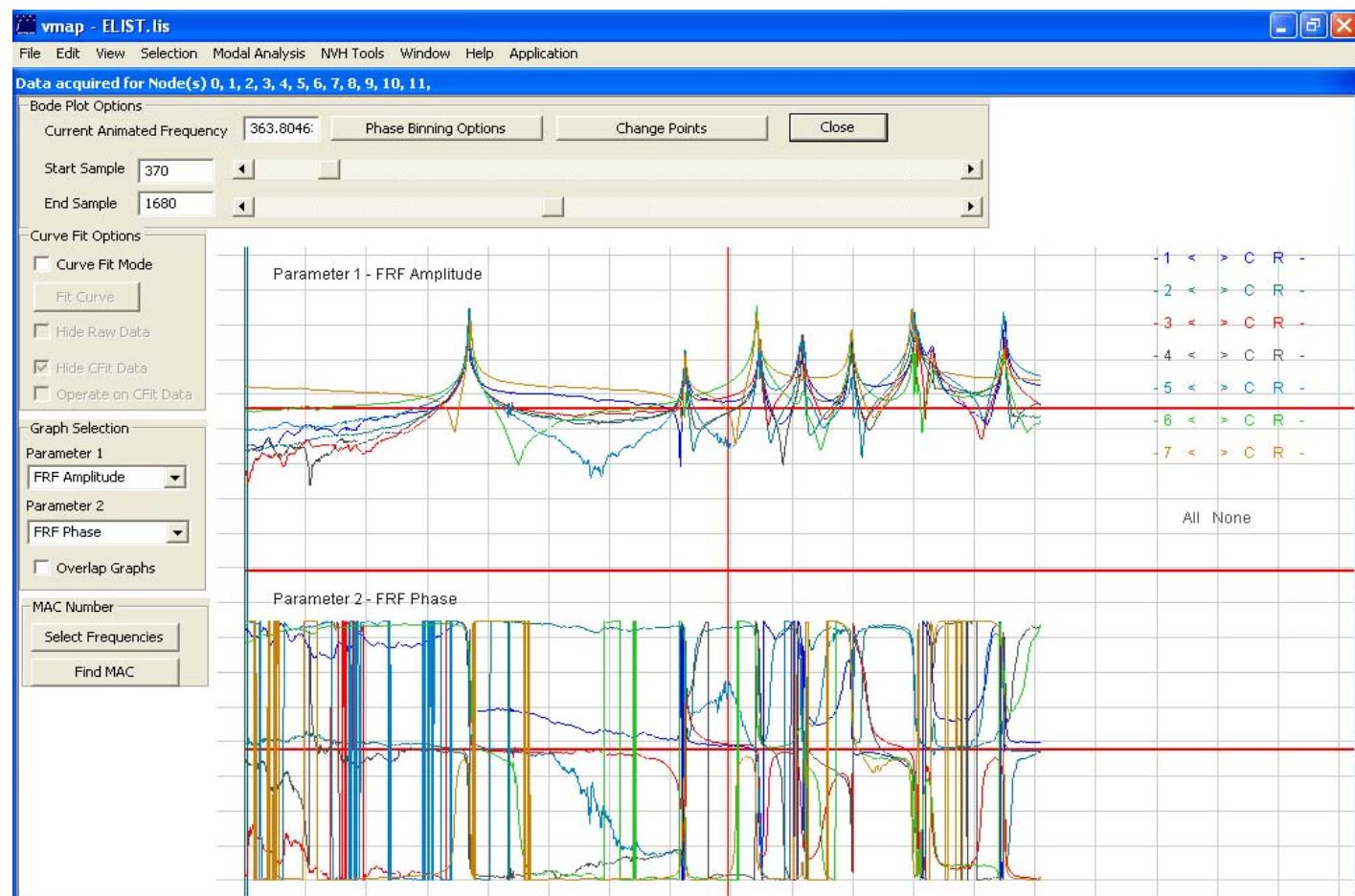
# Repeatability

- To ensure that the whole setup and measurement system is time-invariant
- For a given pair of excitation and measurement locations, an LTI should yield identical FRF for every measurement
- Repeat some FRF measurements at the beginning and end of test

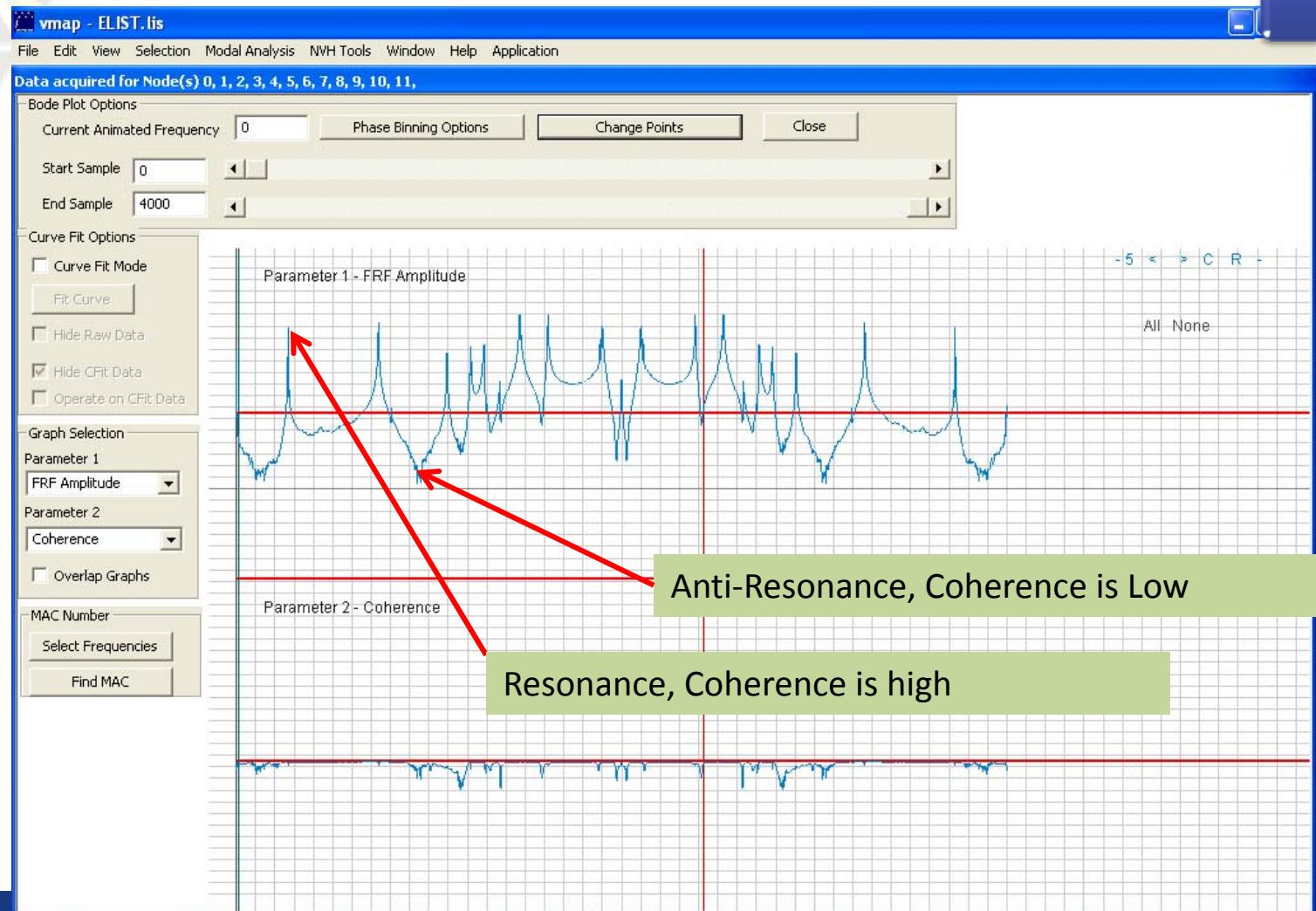


Test

# Modal Parameters



# Coherence



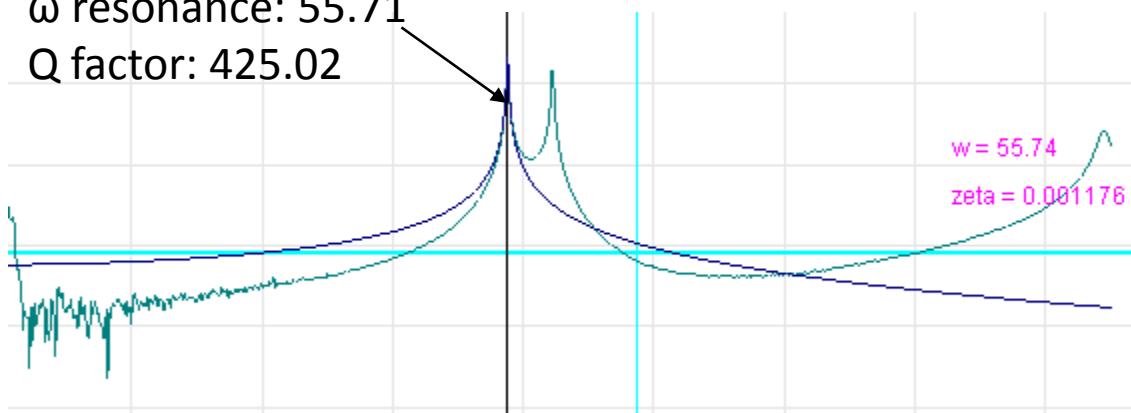
# Modal Parameters

Test

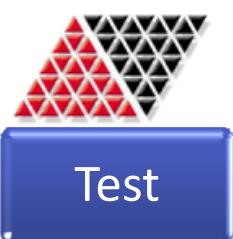
- Damping

$$\zeta = \frac{1}{2Q} = \frac{1}{850} = 0.0012$$

$\omega$  resonance: 55.71  
Q factor: 425.02

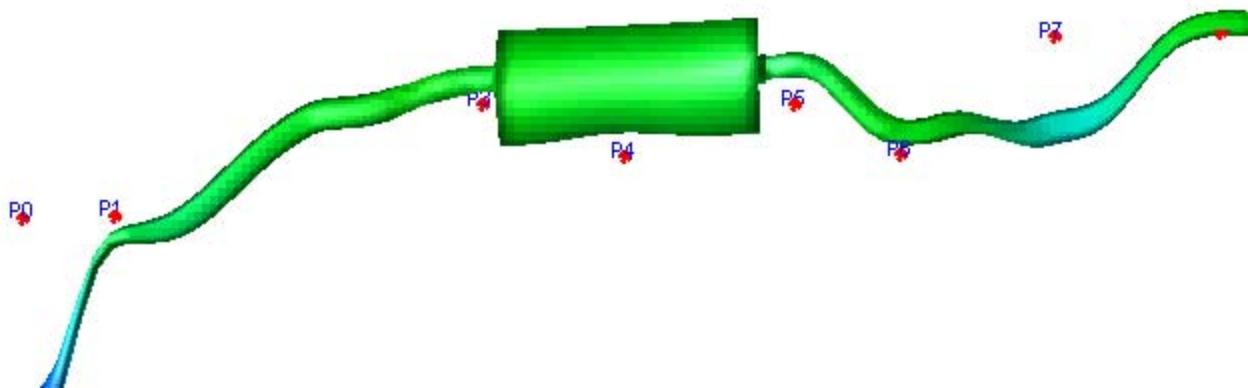


Damping cannot be estimated through FEA – It is estimated only by experimental method

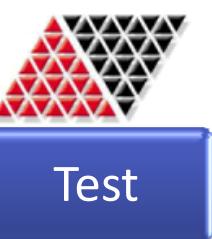


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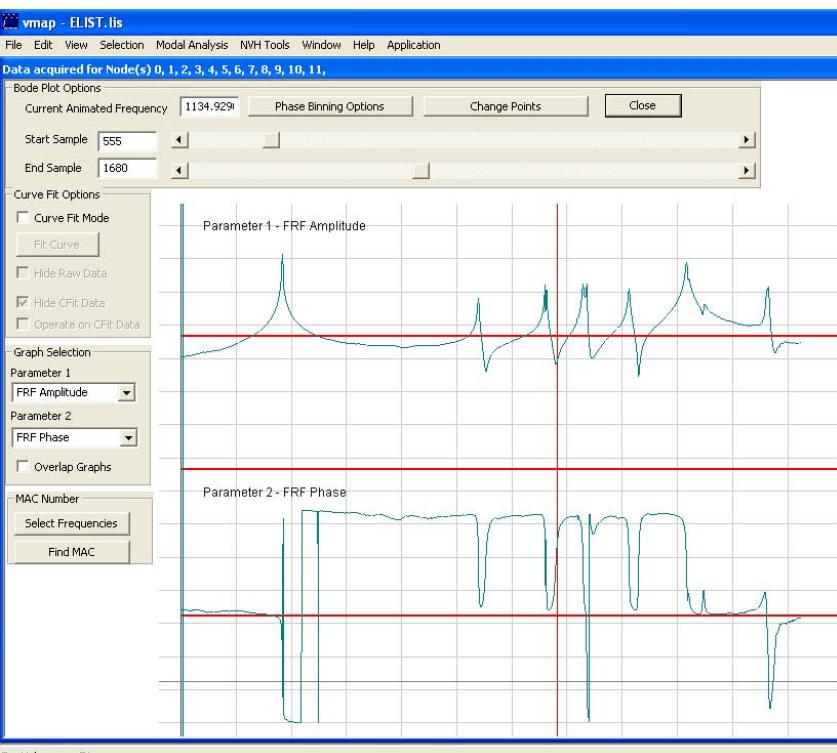
# Modeshapes



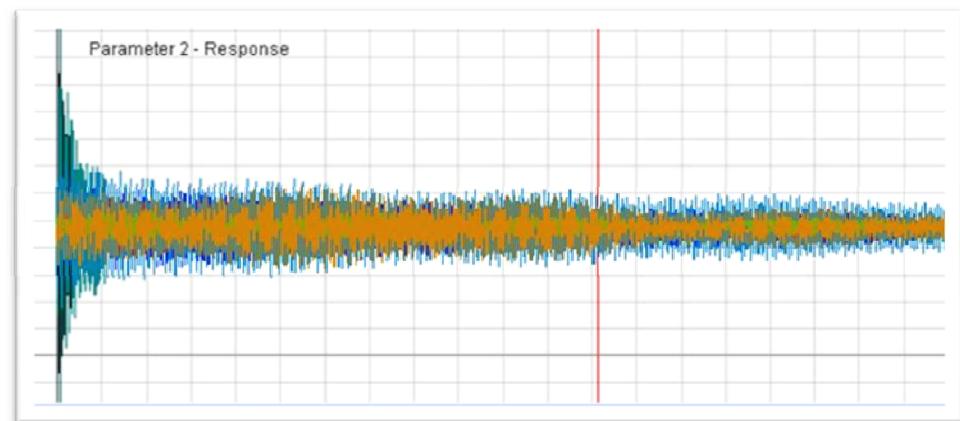
# Modal Parameter Extraction

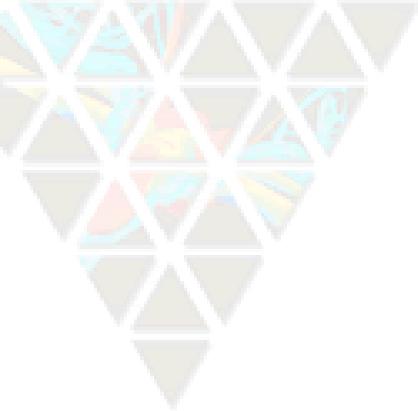


## Frequency Domain Analysis



## Time Domain Analysis





# Comparison

## Time Domain Analysis

Can be done even with ambient excitation

Noise affects the predictions significantly

Needs simultaneous measurement of all channels

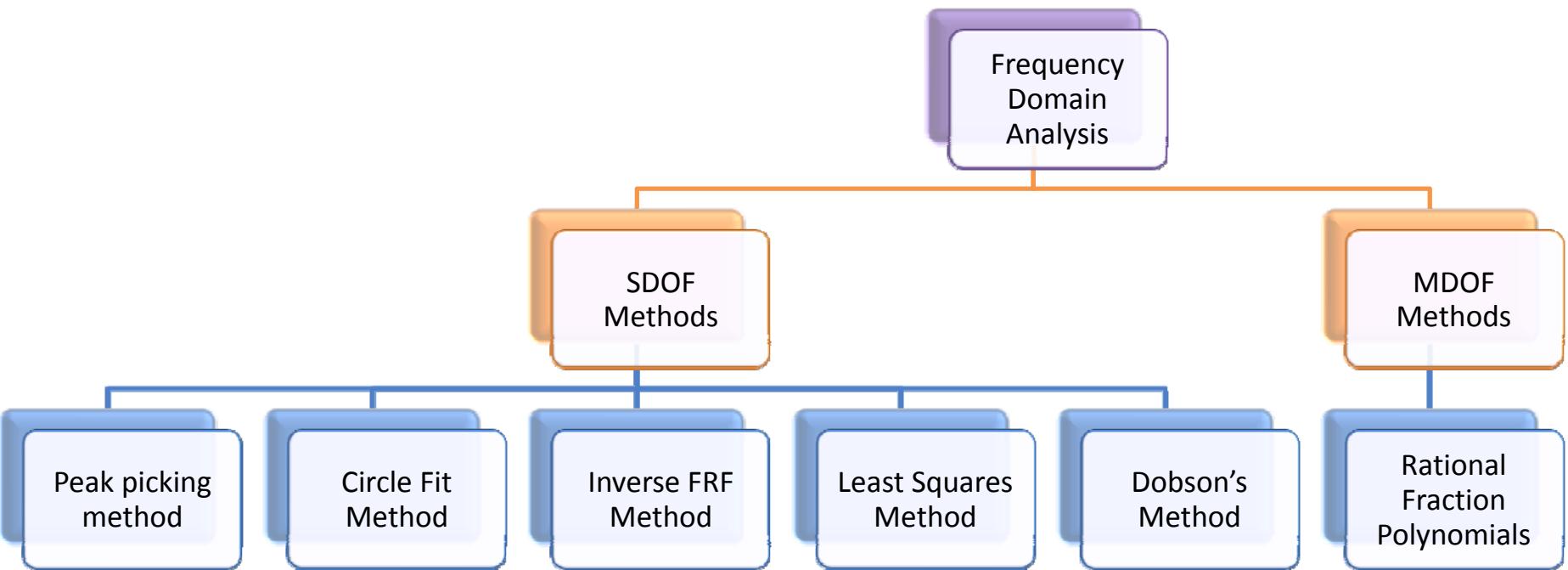
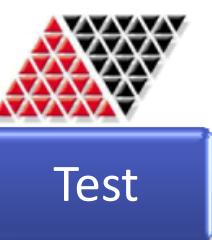
## Frequency Domain Analysis

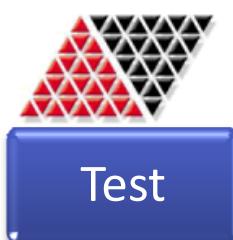
Needs controlled excitation

Effect of noise near resonances is small

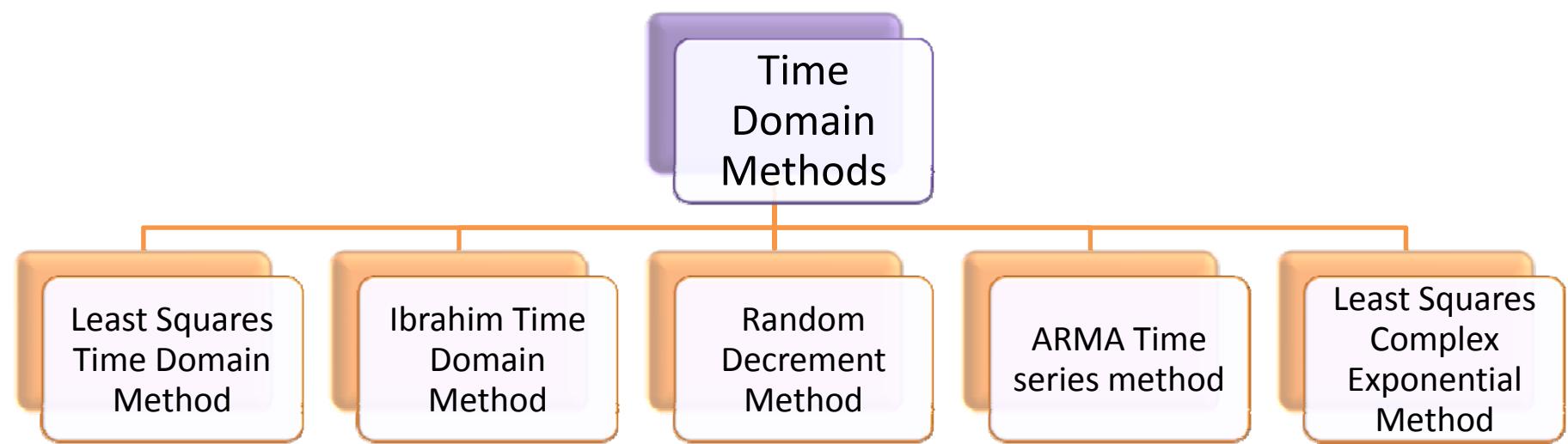
Can be done with one measurement point at a time

# Frequency Domain Methods

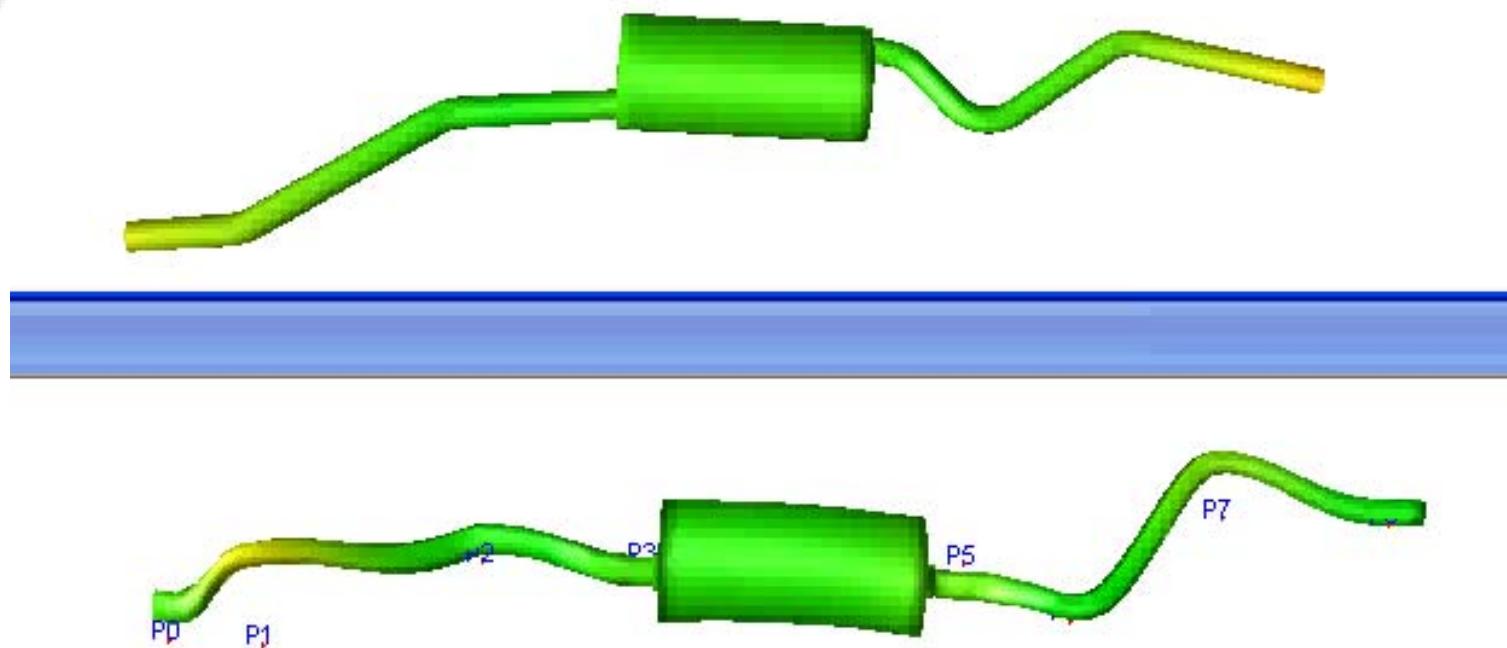




# Time Domain Methods

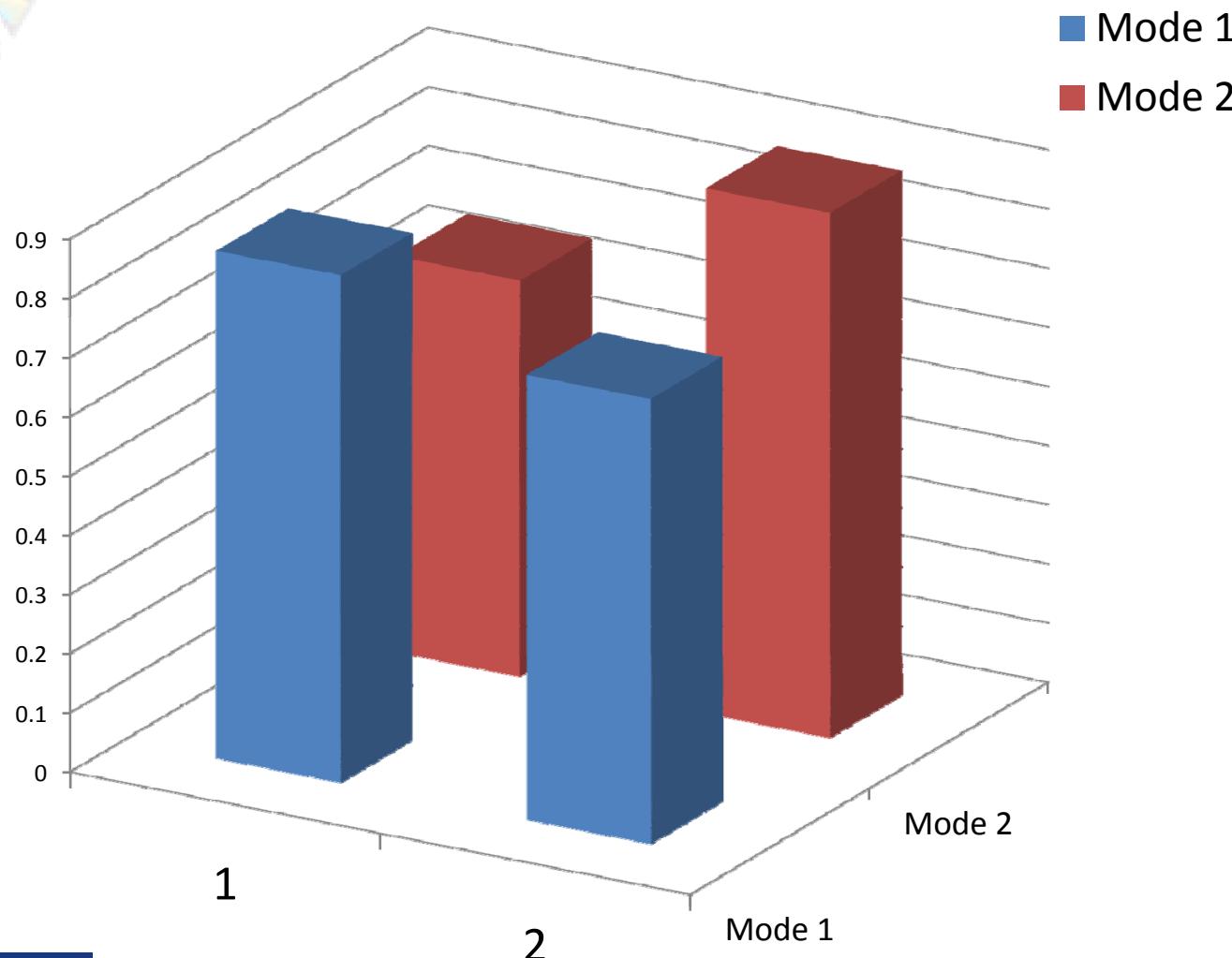


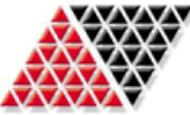
## Simulation Vs Test



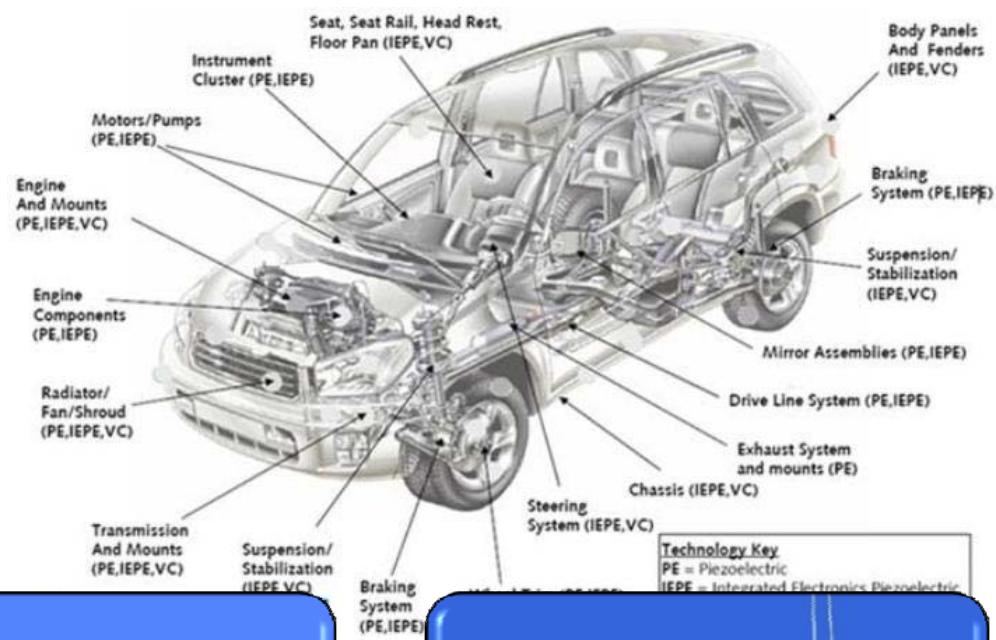


# Modal Assurance Criterion

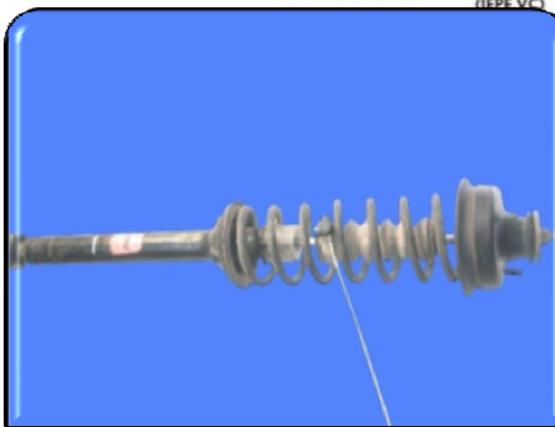




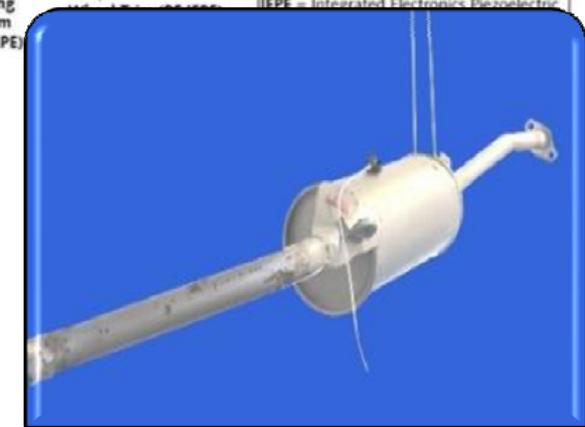
# Automotive



Wheel



Suspension



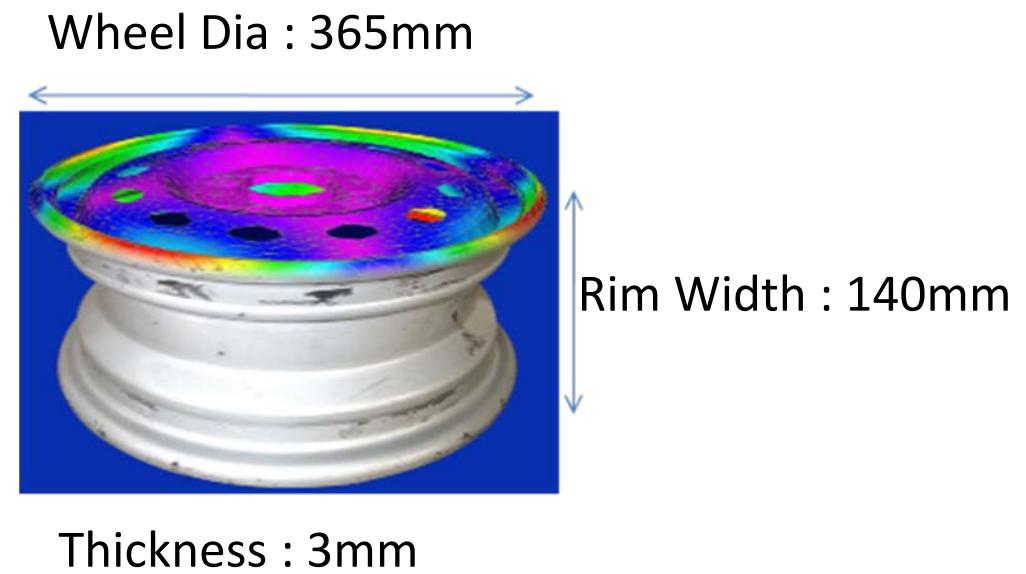
Exhaust

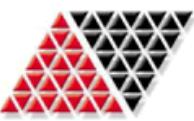




# Case 1: Wheel

- Description
- Finite Element Model
- Experiment
- FEA-Test Correlation
  - Modal Parameters
  - MAC





# Finite Element Model

Mesh

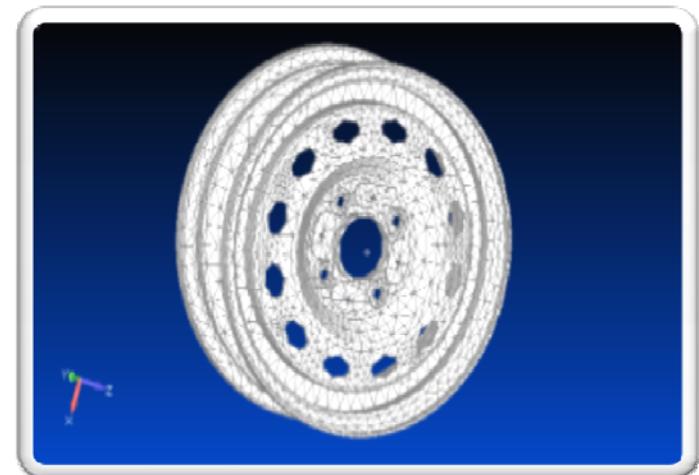
- 10 Node Tetrahedral
- Nodes = 27306
- Elements = 13326

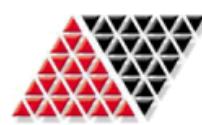
Material

- Aluminum
- Density = 2600 Kg/m<sup>3</sup>
- Young's Modulus = 70e9 N/m<sup>2</sup>
- Poisson's Ratio = 0.3

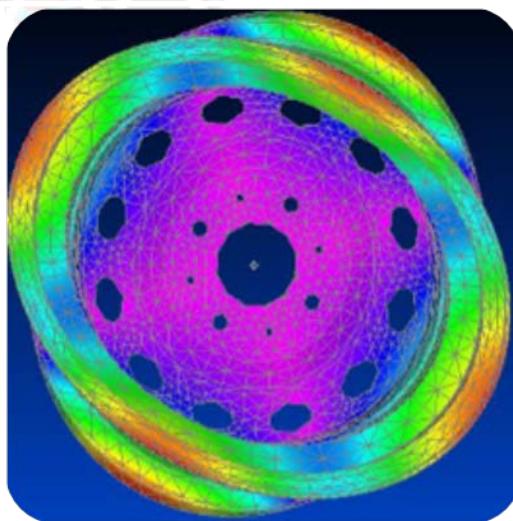
Boundary  
Conditions

- Free - Free



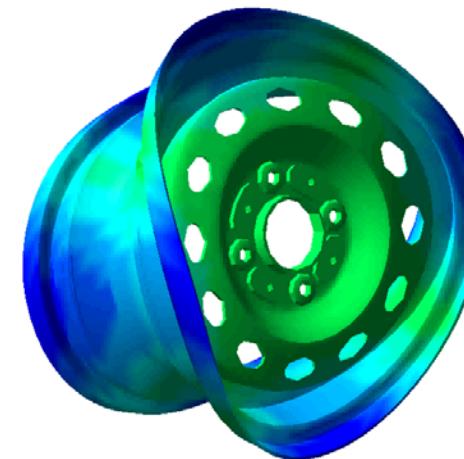


# FEA Results

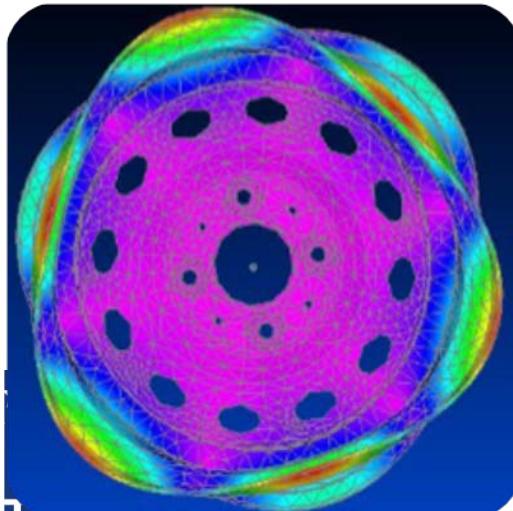


Mode 1 - 311.80 Hz  
Mode 2 – 314.74 Hz

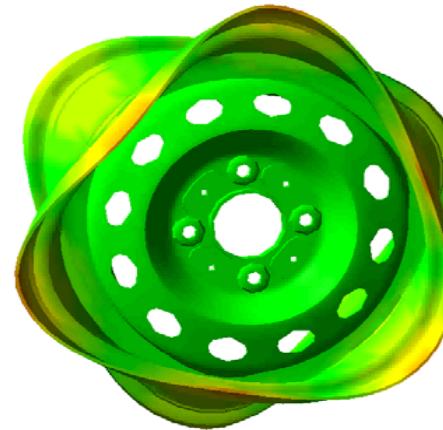
VMAP  
FEA



Animation of Mode 1



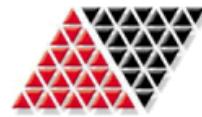
Mode 3 - 893.80 Hz  
Mode 4 - 894.41 Hz



Animation of Mode 3

Animated Frequency = 311.800 Hz  
Mode Number = 1

Animated Frequency = 897.370 Hz  
Mode Number = 3



# Experimental Setup

Data  
Acquisition

- National Instruments USB 9233
- 50 kS/s
- 4 Channels



Stimulus

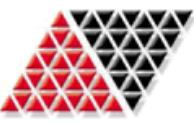
- Impact Hammer
- Range = 500 N
- Sensitivity = 10 mV/N
- Frequency Range < 1200 Hz



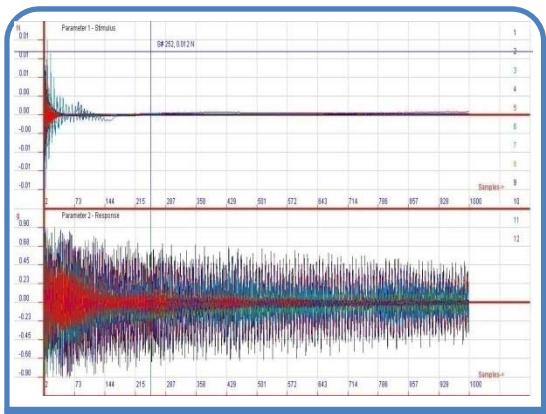
Response

- Accelerometer
- Range : -50g to 50g
- Sensitivity = 100 mV/g

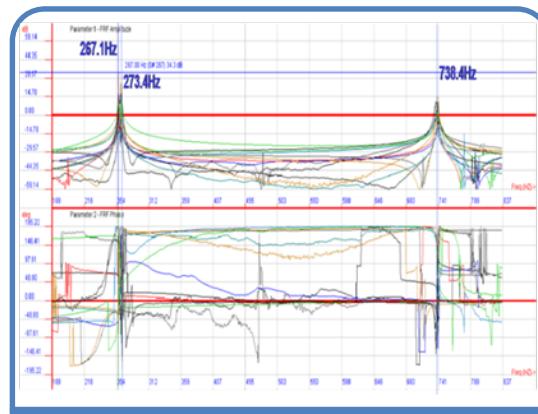




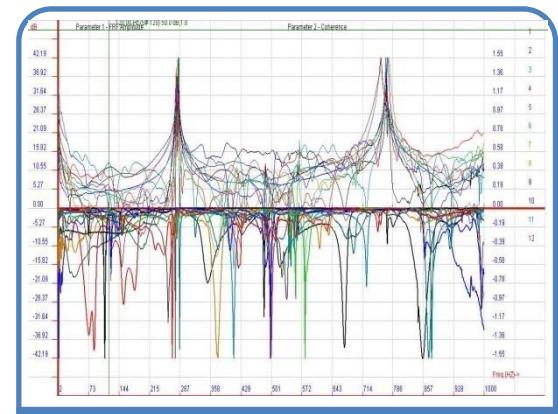
# Test Results



Stimulus and response

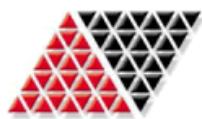


FRF

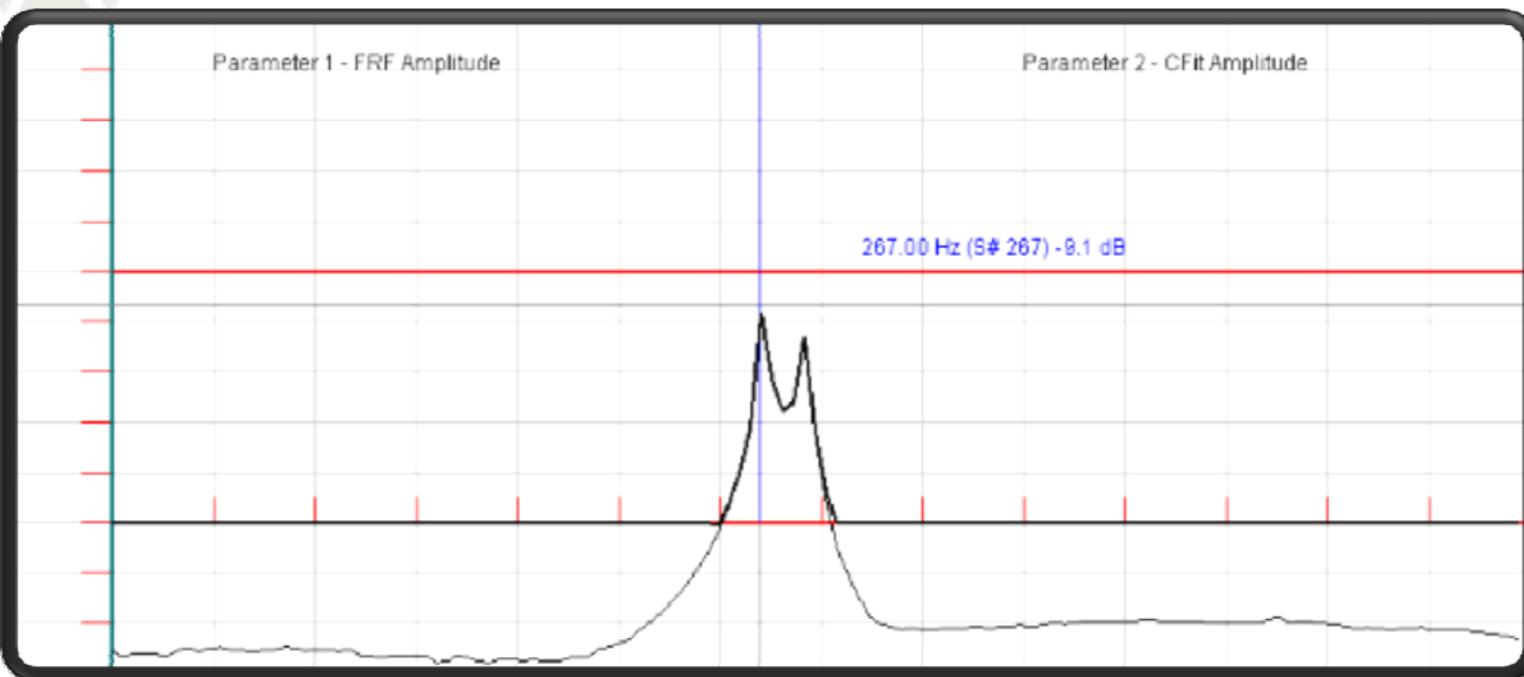


Coherence

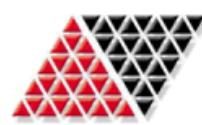




# Curve Fitting



RFP - Identification of Closely Spaced Modes

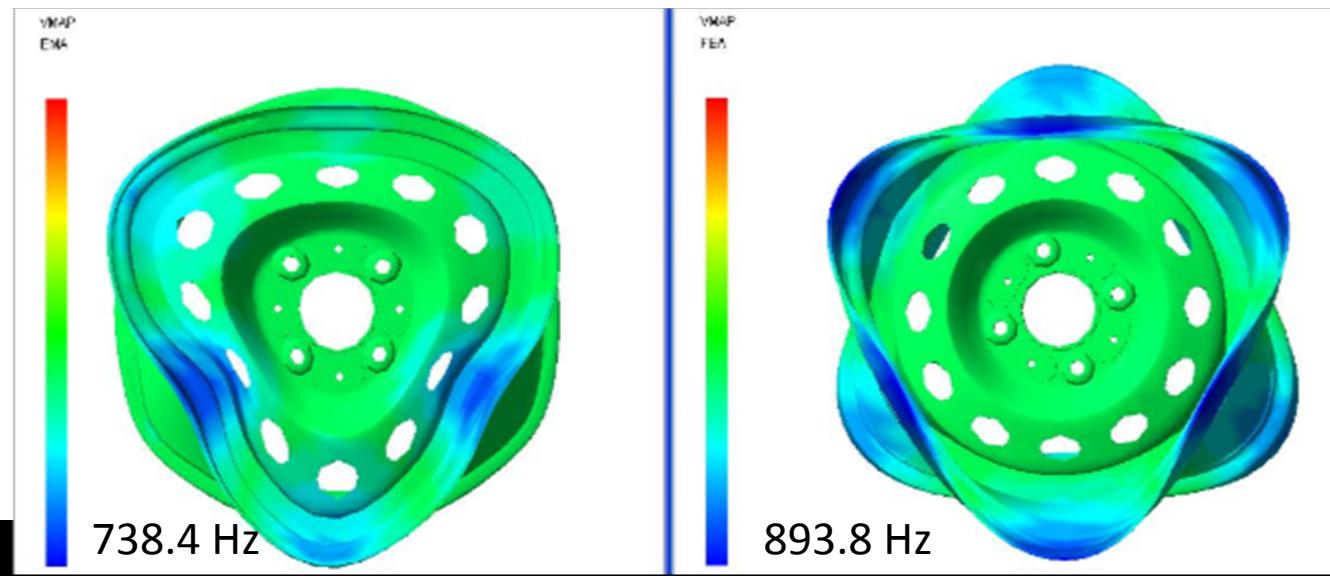
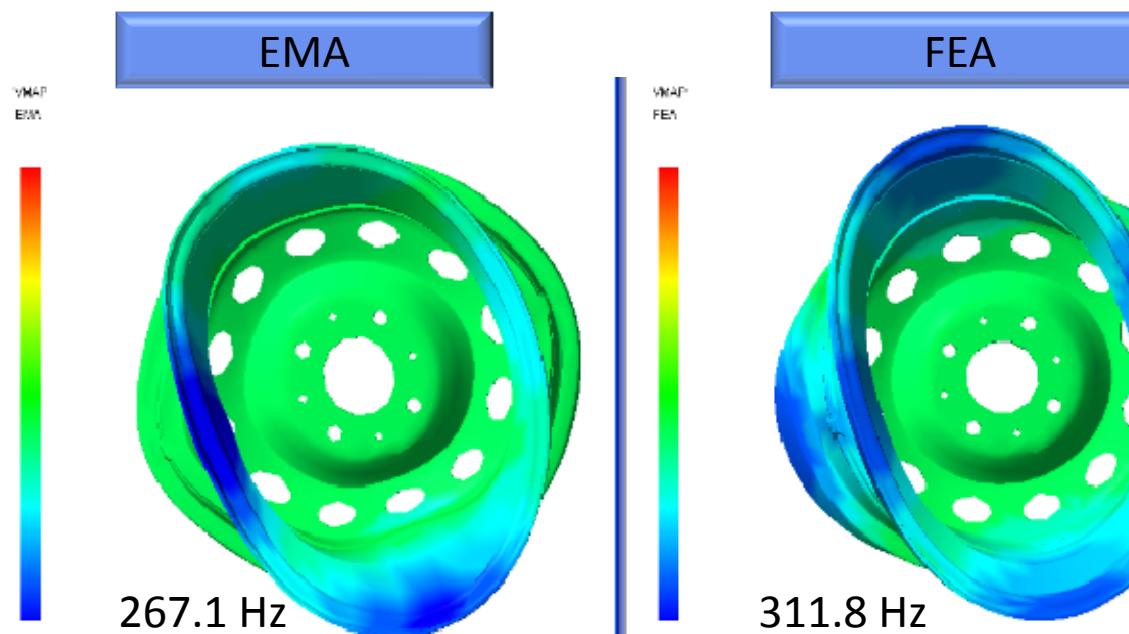
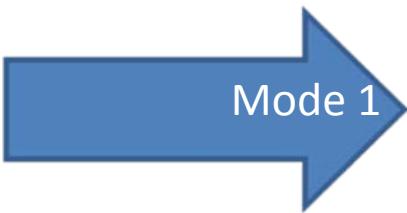
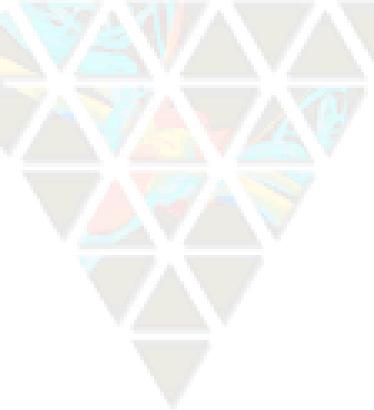
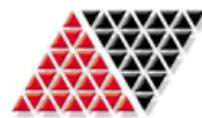


# Modal Parameters

	Rational Fraction Polynomials	
	$\omega_n$ (Hz)	Q Factor
Mode 1	267.1	898.1
Mode 2	273.4	620.4
Mode 3	738.4	491.4

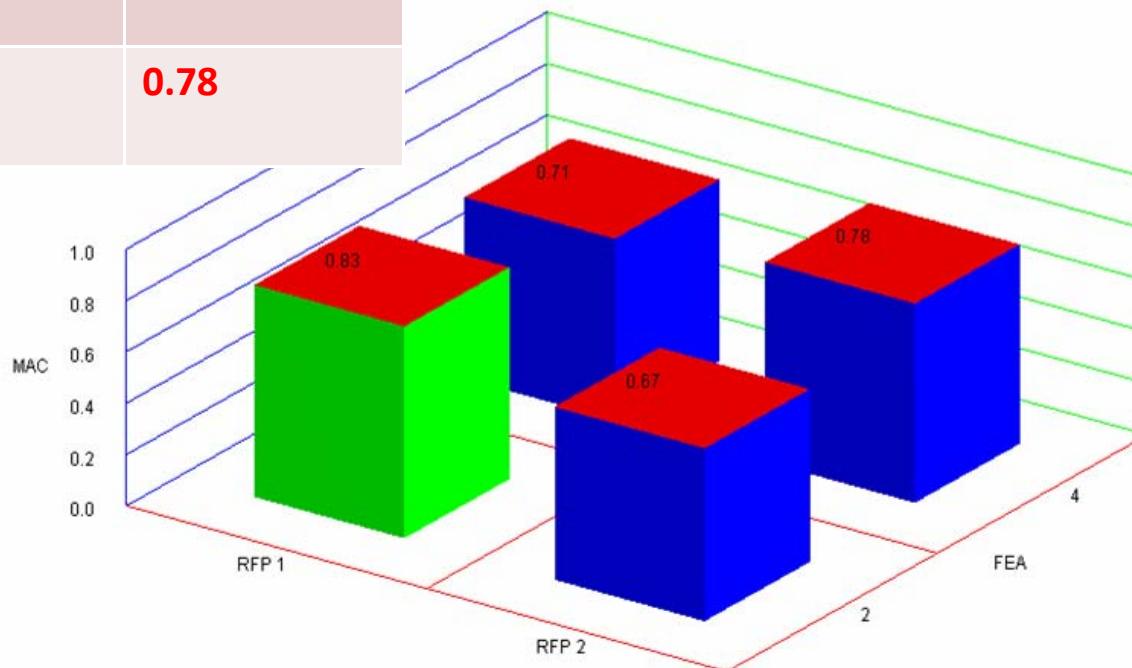


# FEA-Test Correlation



# MAC

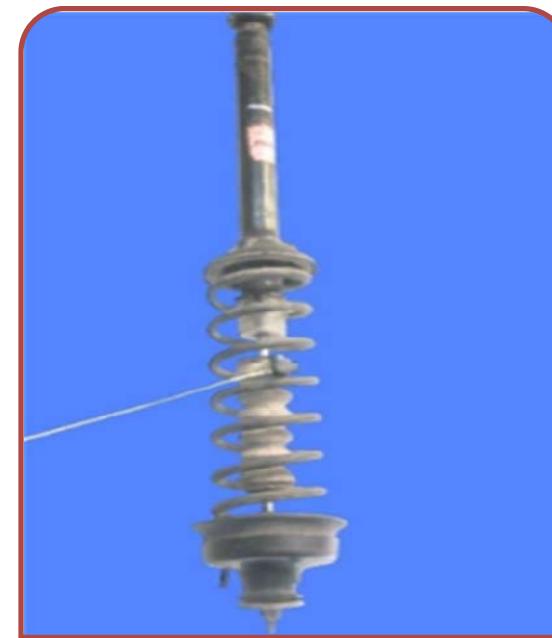
Mode (frequency)	FEA 1 (311 Hz)	FEA 2 (893 Hz)
EMA 1 (267.1 Hz)	<b>0.83</b>	0.71
EMA 3 (738.4 Hz)	0.67	<b>0.78</b>





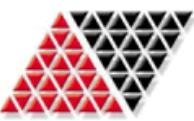
# Case 2: Suspension

- Description
- Finite Element Model
- Experiment
- FEA-Test Correlation
  - Modal Parameters
  - MAC

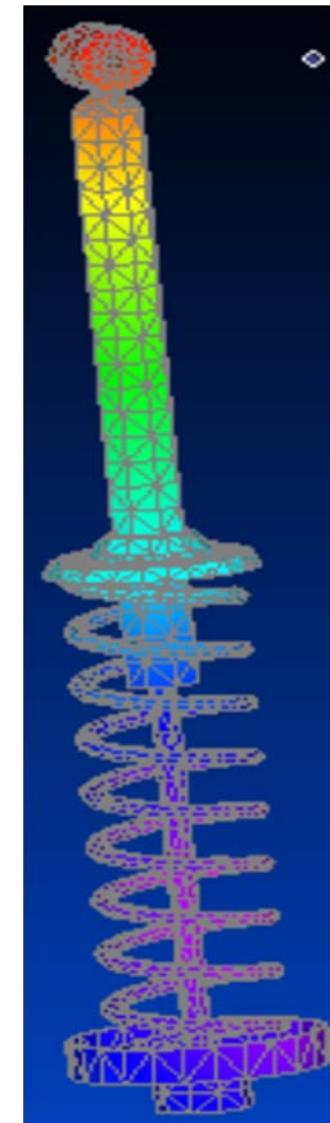
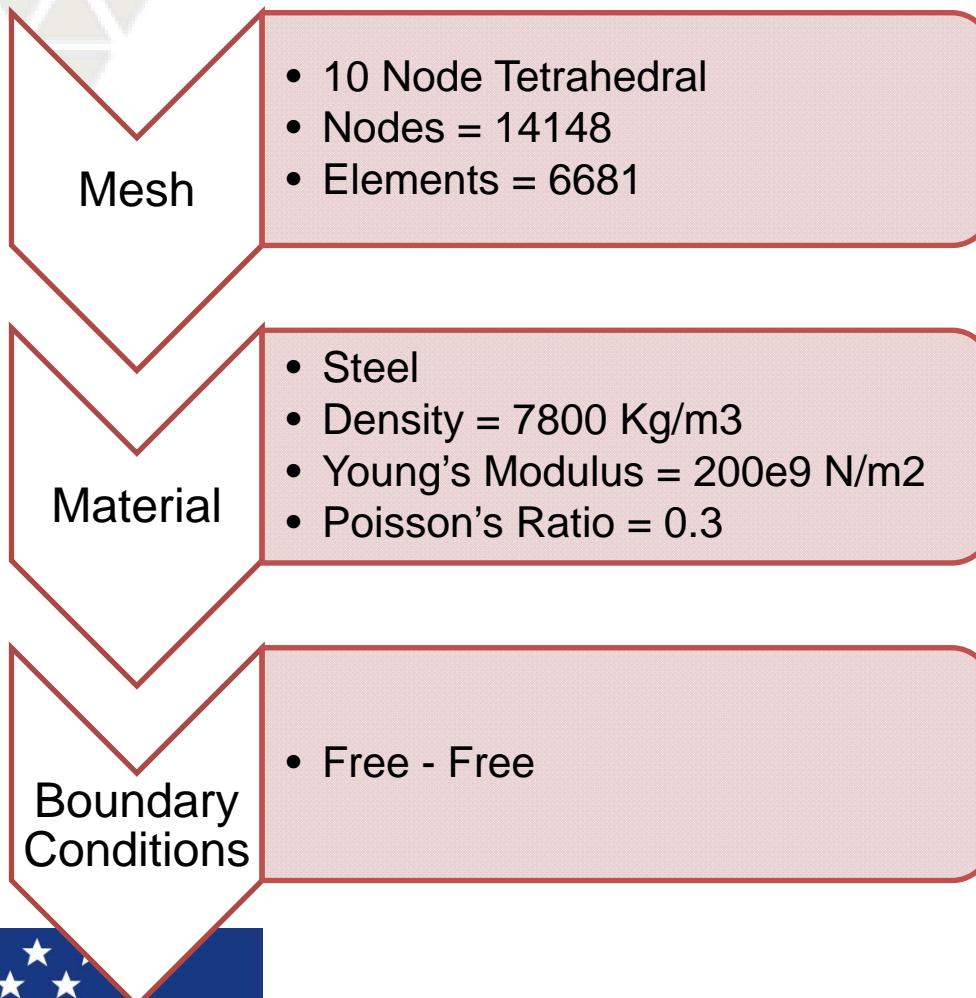


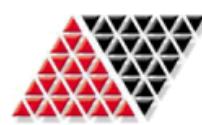
## Suspension



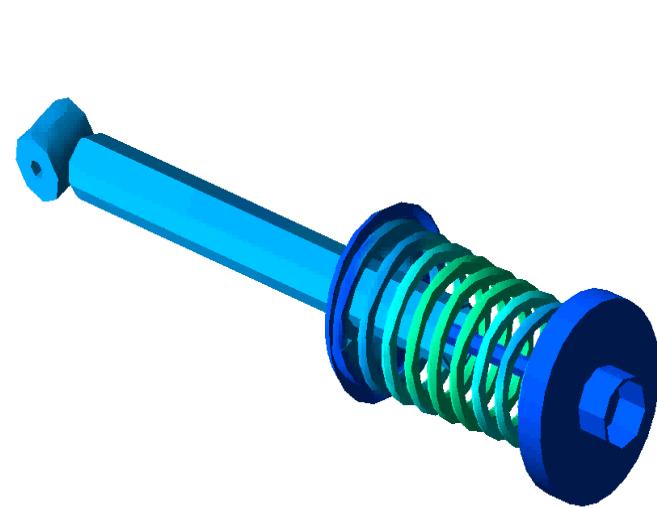
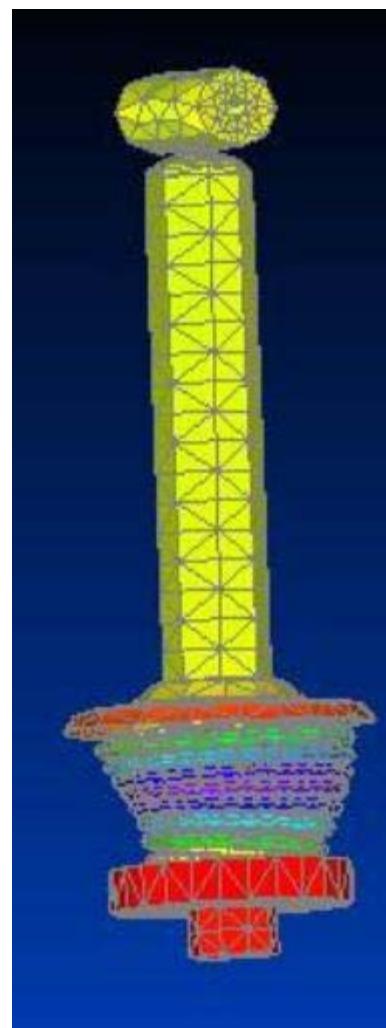


# Finite Element Model

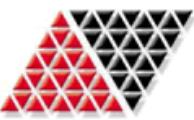




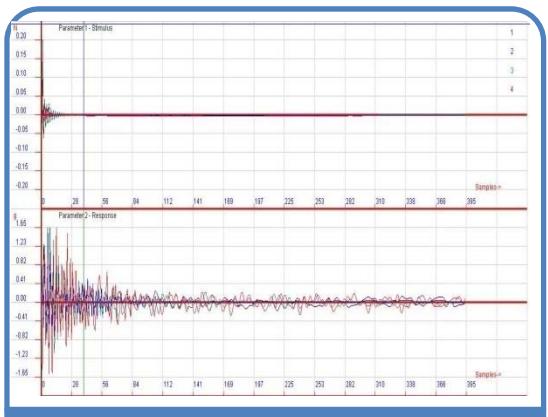
# FEA Results



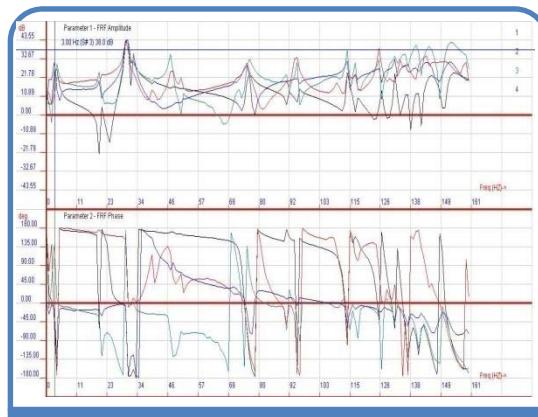
Animation of Mode 1



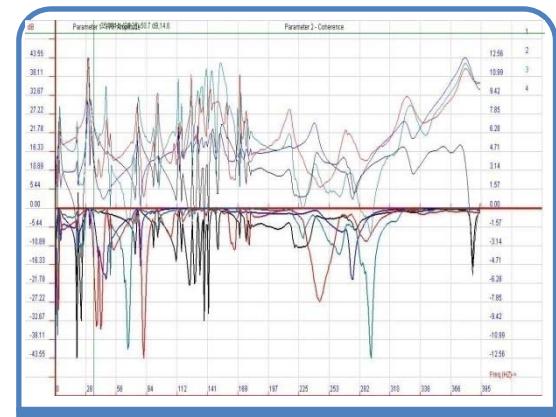
# Test Results



Stimulus and response



FRF

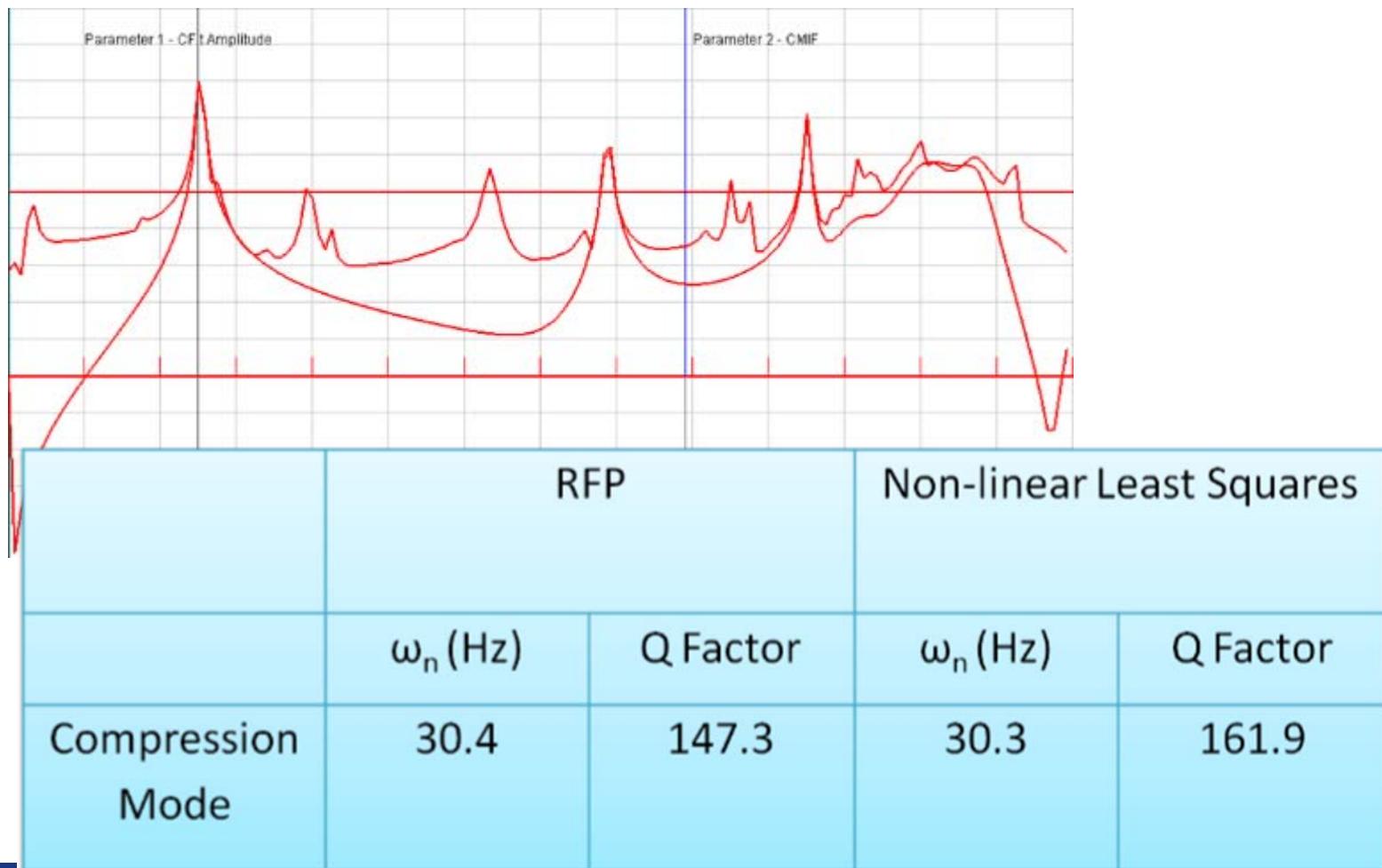


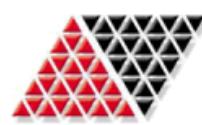
Coherence



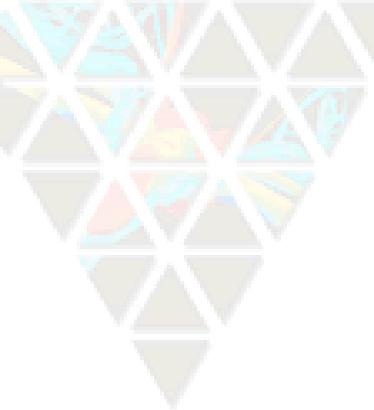


# Modal Parameters

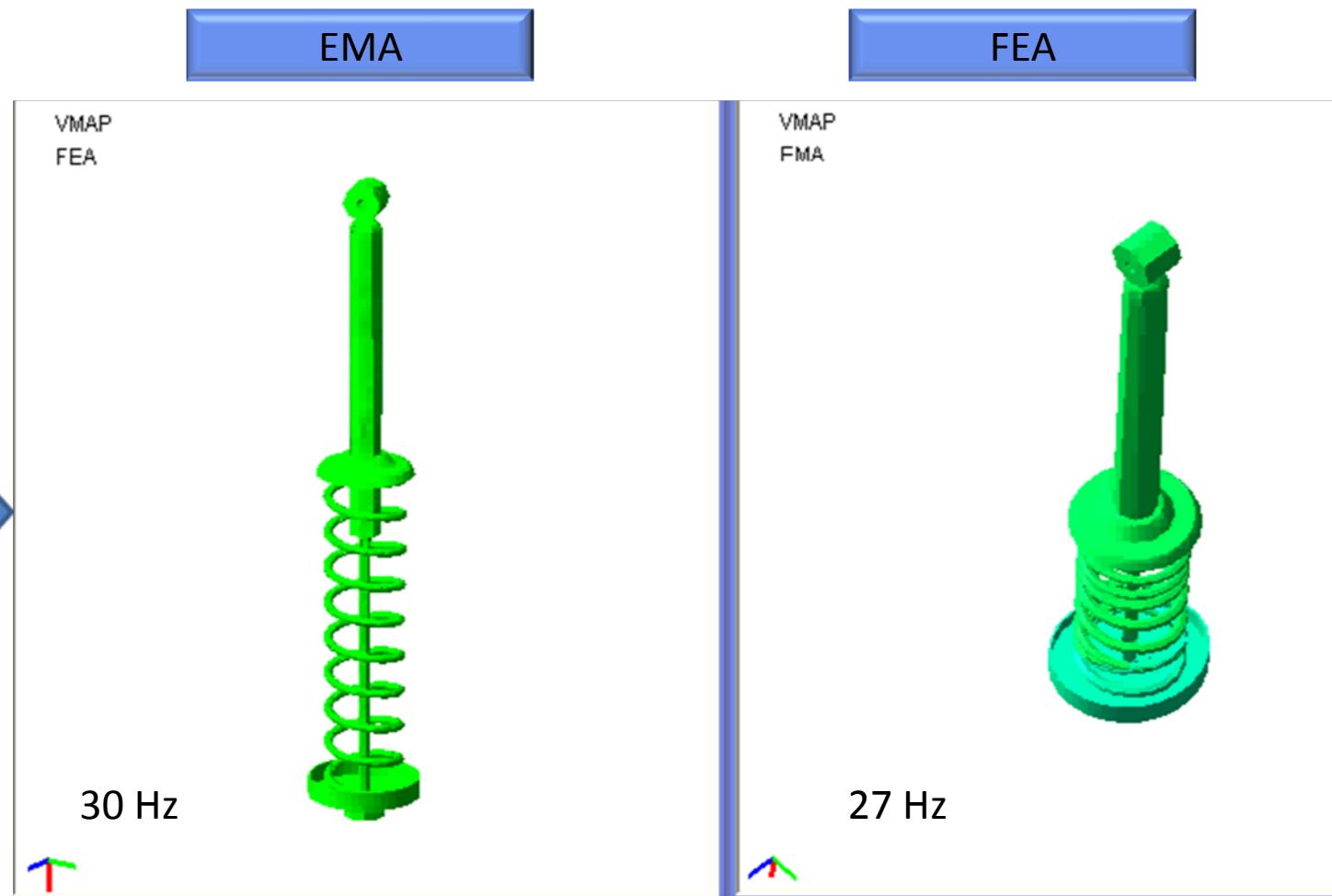




# FEA-Test Correlation



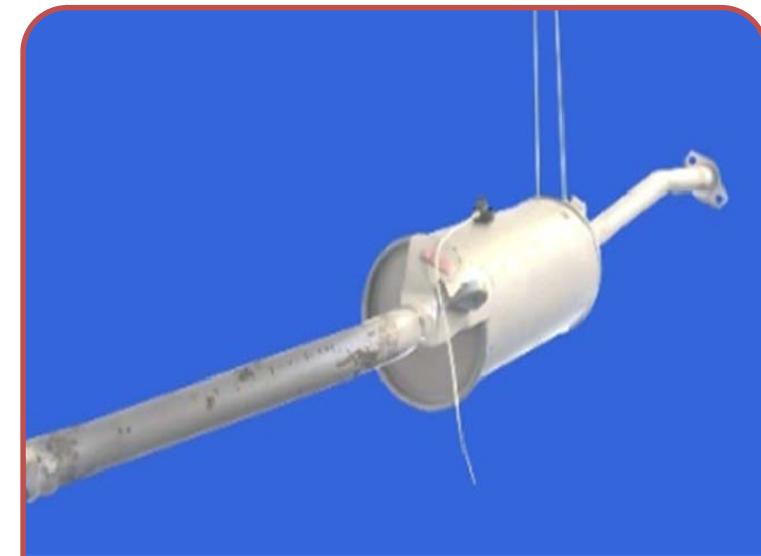
Compression Mode





# Case 3: Exhaust System

- Description
- Finite Element Model
- Experiment
- FEA-Test Correlation
  - Modal Parameters
  - MAC



## Exhaust



# FEA

Mesh

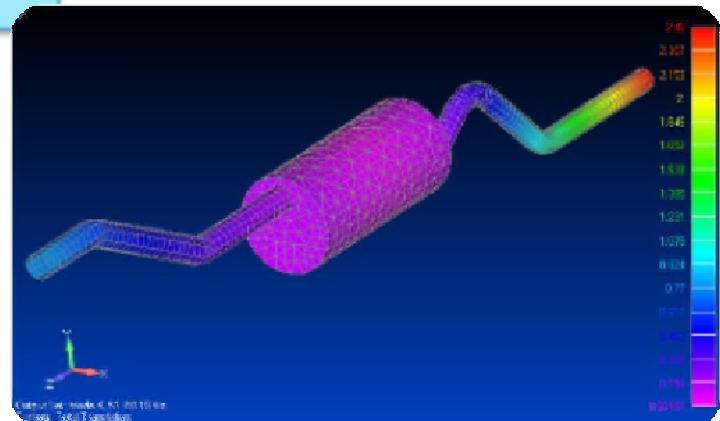
Material

Boundary  
Conditions

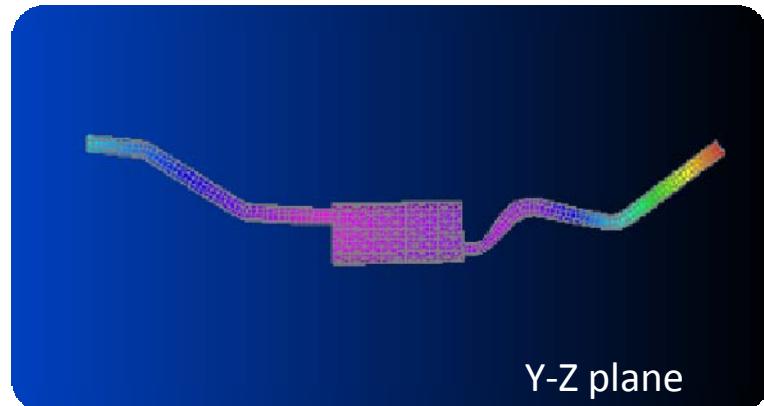
	Type
Engine Manifold	<ul style="list-style-type: none"><li>• 4 Node, Plate</li><li>• 6 per node</li></ul>
Drum	<ul style="list-style-type: none"><li>• 10 Node, Solid</li><li>• 3 per node</li></ul>
Exhaust Manifold	<ul style="list-style-type: none"><li>• 4 Node, Plate</li><li>• 6 per node</li></ul>

	Material
Engine Manifold	$E=1.9e11 \text{ N/m}^2$ $\rho=8000 \text{ Kg/m}^3$ $\nu=0.3$
Drum	$E=2.1e11 \text{ N/m}^2$ $\rho=1000 \text{ Kg/m}^3$ $\nu=0.3$
Exhaust Manifold	$E=1.9e11 \text{ N/m}^2$ $\rho=8000 \text{ Kg/m}^3$ $\nu=0.3$

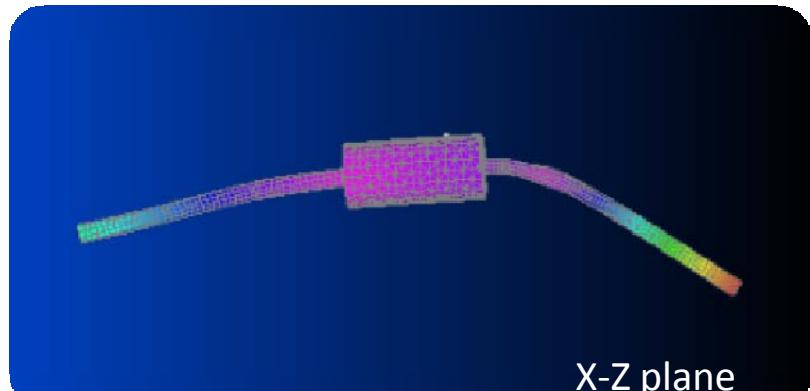
Free - Free



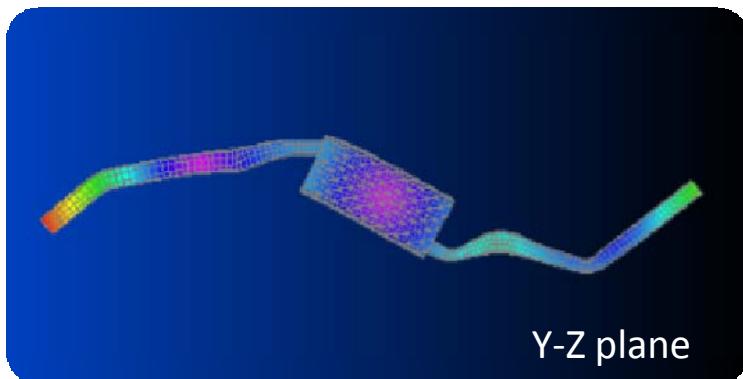
# FEA Results



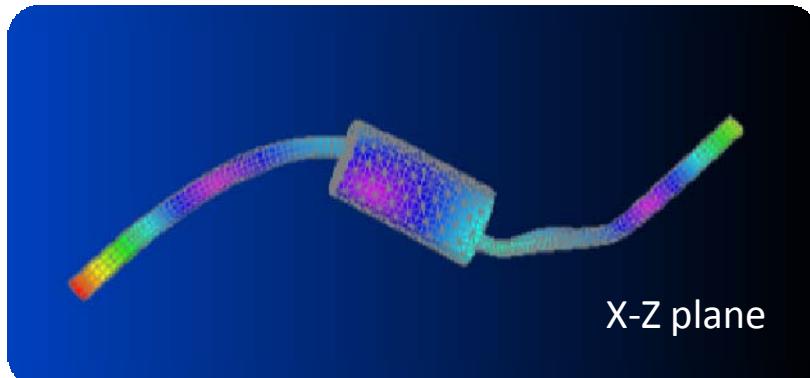
Mode 1 = 58.96 Hz



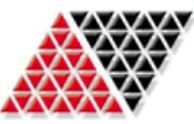
Mode 2 = 63.18 Hz



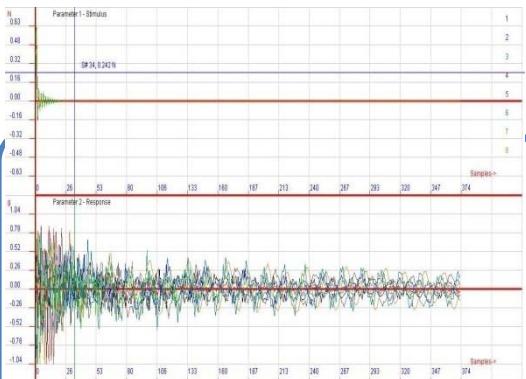
Mode 3 = 142.91 Hz



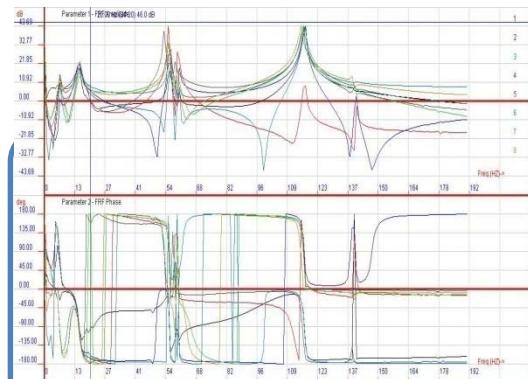
Mode 4 = 162.32 Hz



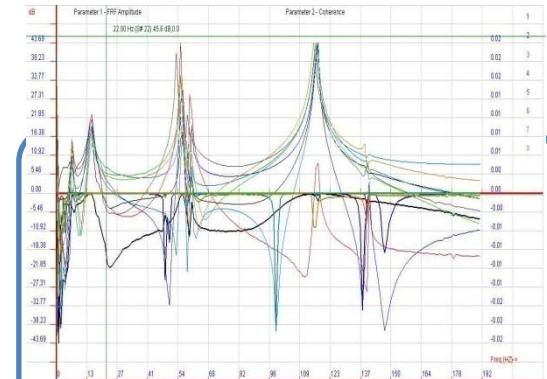
# Test Results



Stimulus and response



FRF

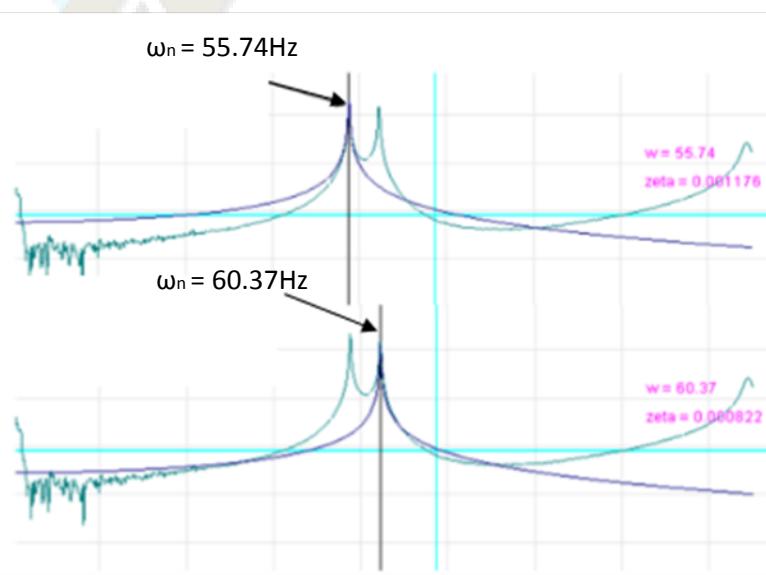


Coherence



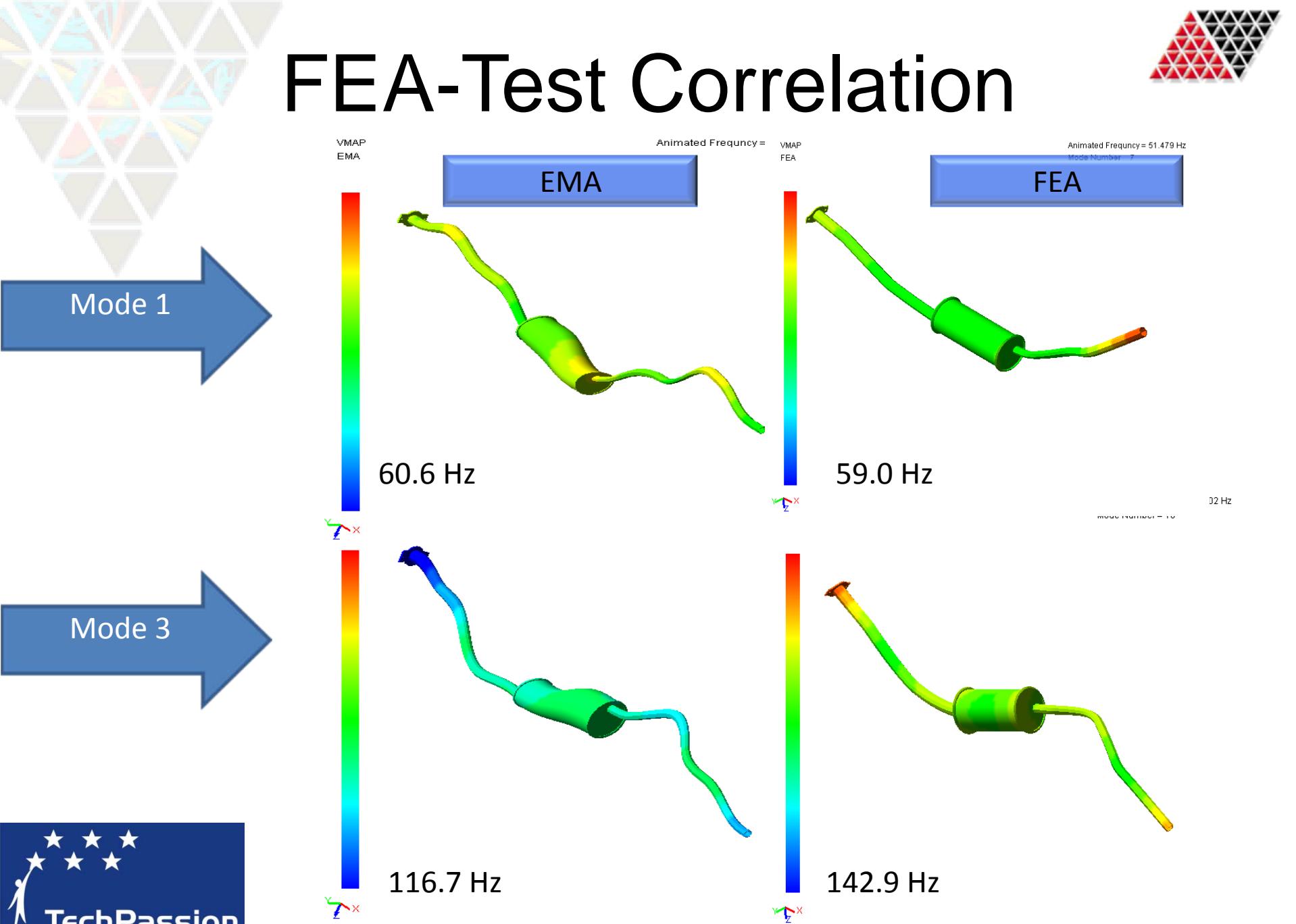


# Modal Parameters



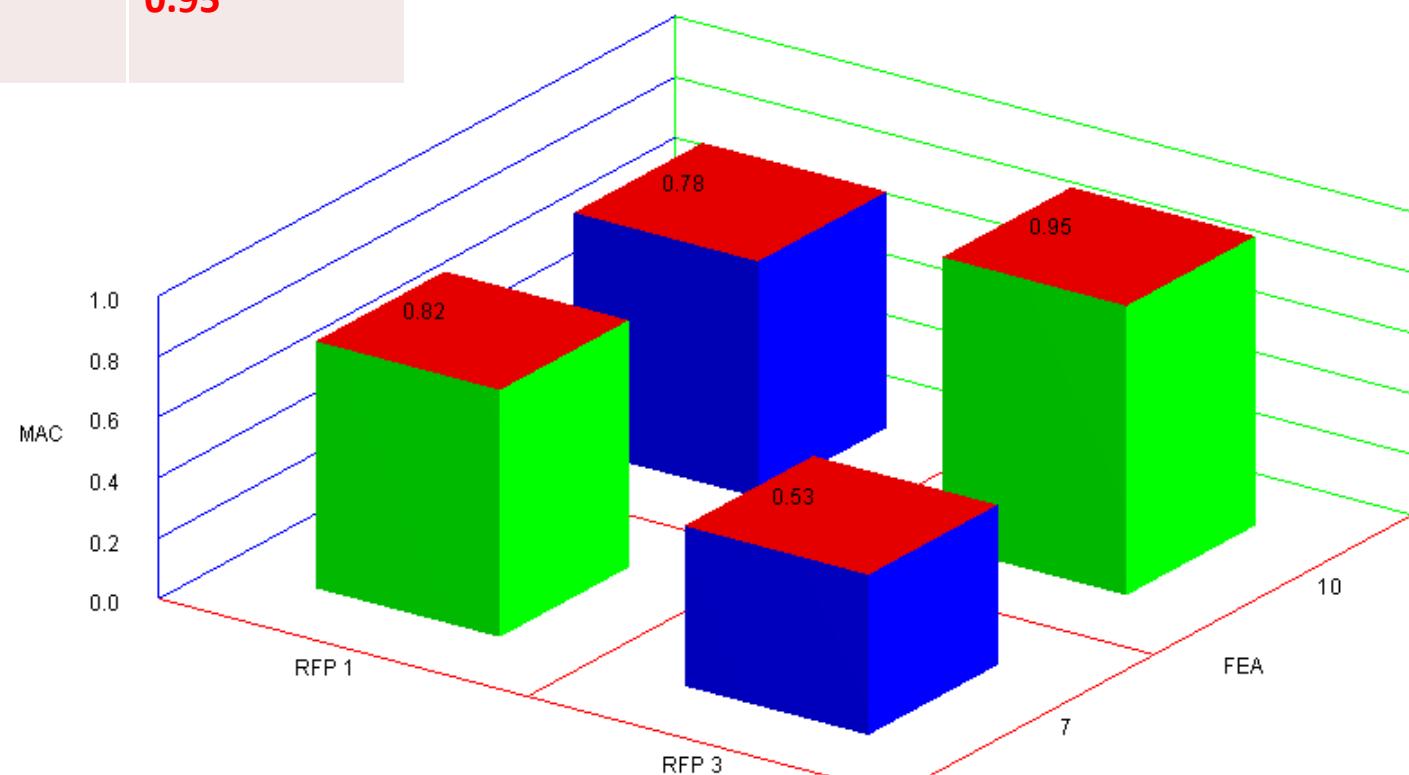
	Circle Fit		RFP	
	$\omega_n$ (Hz)	Q Factor	$\omega_n$ (Hz)	Q Factor
Mode 2	60.34	608.27	60.61	618.65
Mode 3	116.59	88.21	116.67	86.51

# FEA-Test Correlation



# MAC

Mode (frequency)	FEA 1 (51.5 Hz)	FEA 3 (130.7 Hz)
EMA 1 (56.2 Hz)	<b>0.82</b>	0.78
EMA 3 (116 Hz)	0.53	<b>0.95</b>





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## Q&A Session

Using the Q&A tool, please submit any questions you may have for our panel.



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# Thank you!

[matthew.ladzinski@nafems.org](mailto:matthew.ladzinski@nafems.org)